

# V. Exploring Propagating Microwaves with Linear Detectors

- Correlation Function Measurements
- Quantum State Tomography
- Qubit Photon Entanglement
- Two-Mode Entanglement

# Exploring the Properties of Propagating Photons

quantum optics in the **visible**:

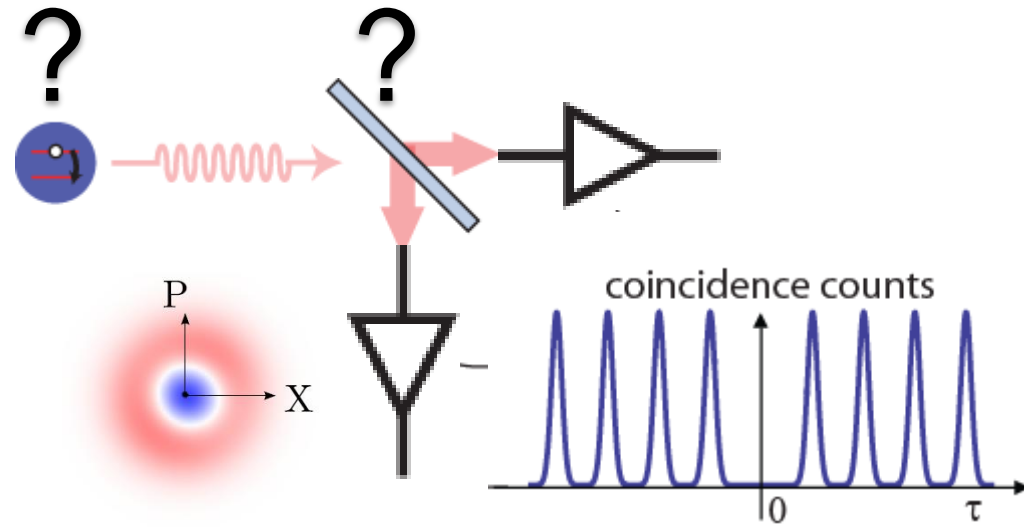
- single photon sources
- beam splitters
- photon counters

o.k. at **optical frequencies**

But in the **microwave domain**?

- smaller photon energy ...

$$\frac{\nu_{\text{opt}}}{\nu_{\mu\text{w}}} = \frac{500 \text{ THz}}{5 \text{ GHz}} = 10^5$$



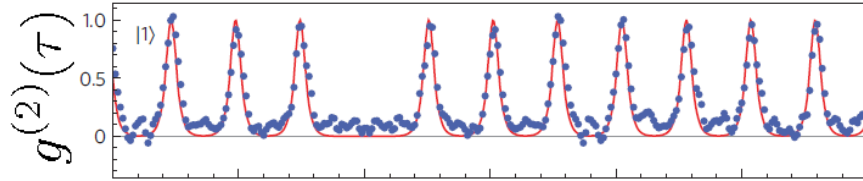
instead:

- linear amplifiers
- signal processing

J. Gabelli et al., *Phys. Rev. Lett.* **93**, 056801 (2004)  
E. P. Menzel et al., *Phys. Rev. Lett.* **105**, 100401 (2010)  
M. P. da Silva et al., *Phys. Rev. A* **82**, 043804 (2010)  
C. Eichler et al., *Phys. Rev. A* **86**, 032106 (2012)

# Experiments with Propagating Quantum Microwaves

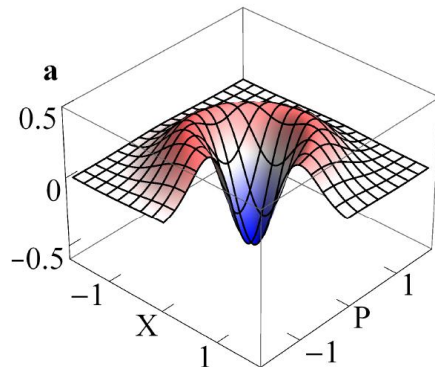
Single photon sources and their anti-bunching



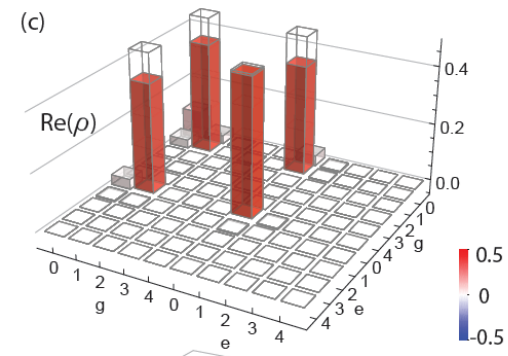
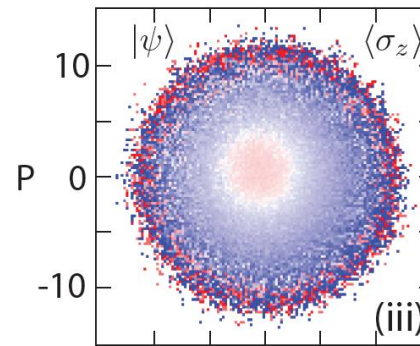
Bozyigit *et al.*, *Nat. Phys* 7, 154 (2011)  
Lang *et al.*, *PRL* 107, 073601 (2011)

Wigner functions and full state tomography of propagating photons

Eichler *et al.*, *PRL* 106, 220503 (2011)



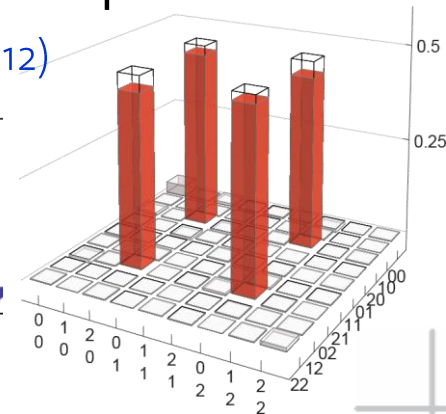
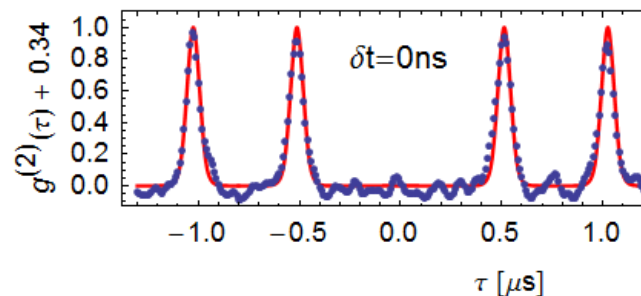
Preparation and characterization of qubit-propagating photon entanglement



Eichler *et al.*, *arXiv:1209.0441* (2012)  
Eichler *et al.*, *Phys. Rev. A* 86, 032106 (2012)

Hong-Ou-Mandel: Two-photon interference with coherences at microwave frequencies

Lang, Eichler *et al.*, *ETH Zurich* (2012)

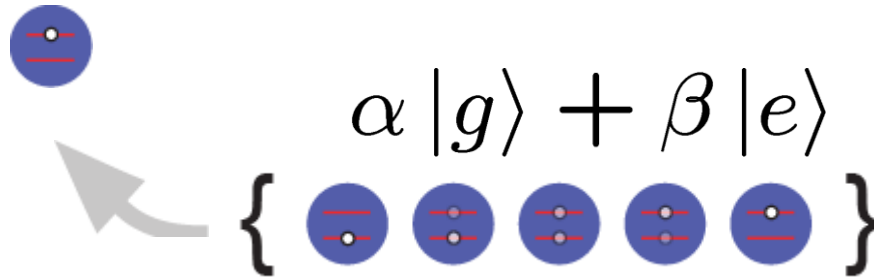
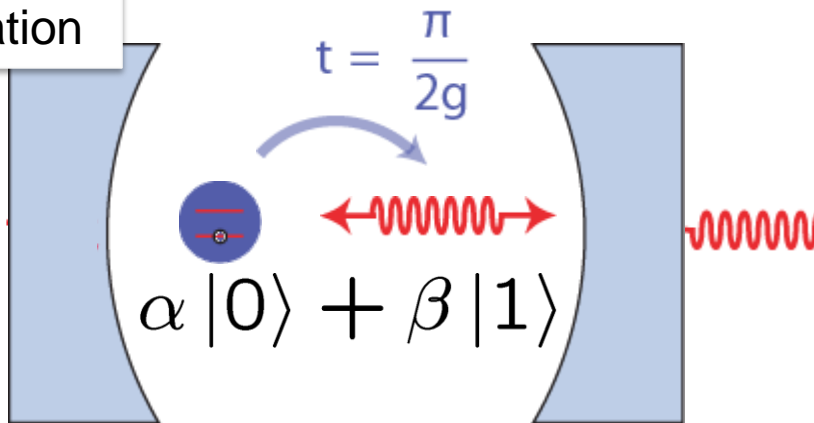


# Single Pulsed Photon Source and Beam-Splitter

# On-Demand Pulsed Single Photon Source

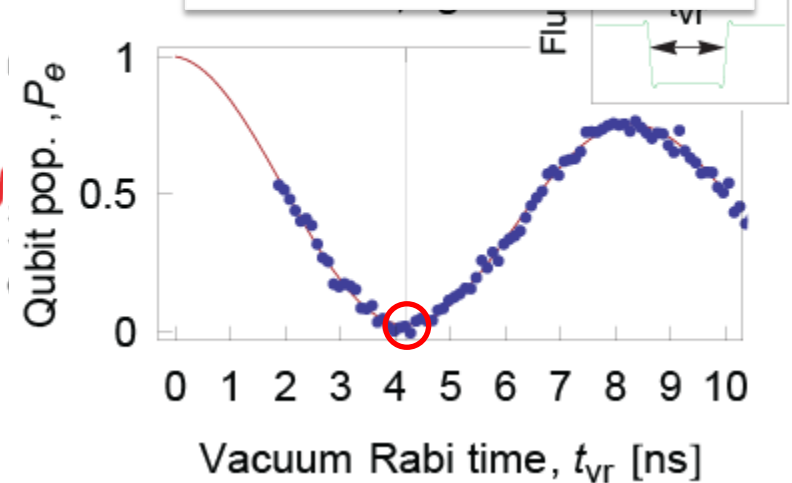
## Step 2:

Map qubit state to resonator by 1/2 vacuum Rabi oscillation



## Step 3:

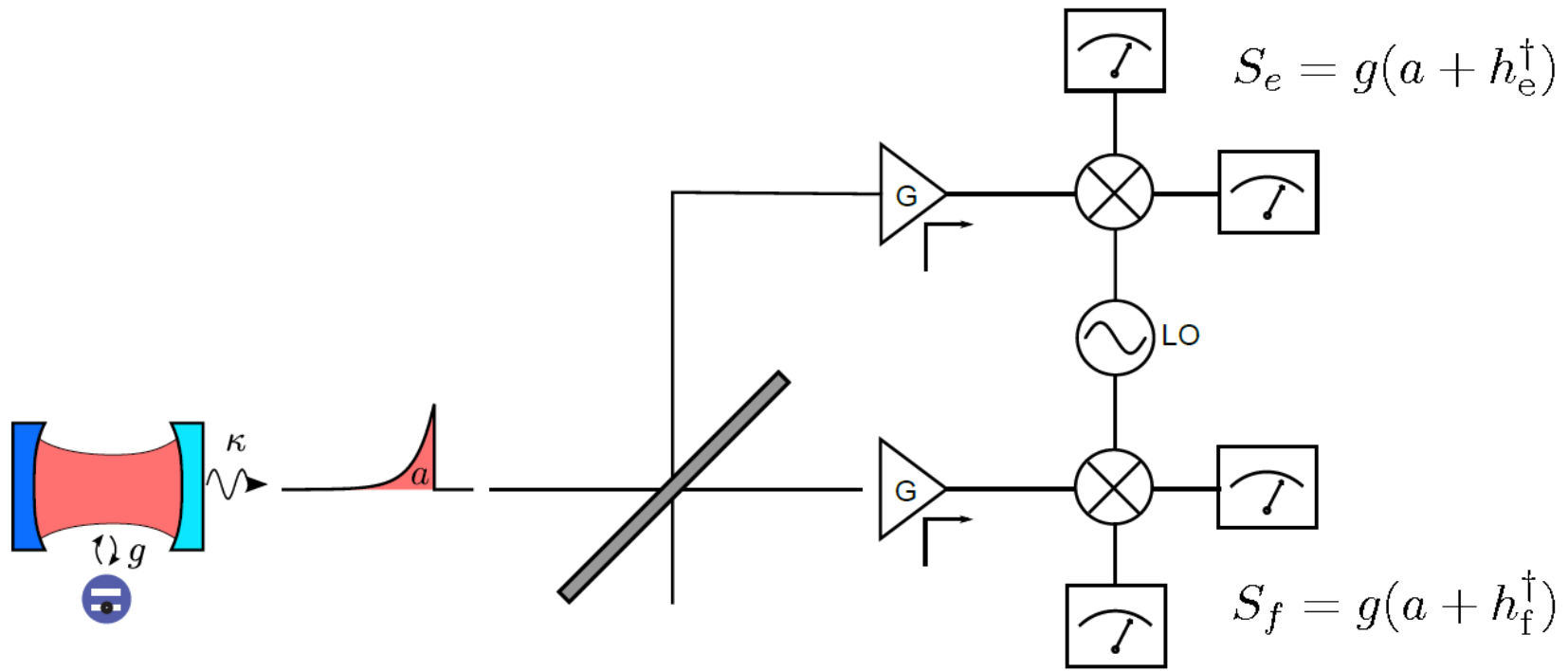
Measure at the output using linear amplifier and signal processing hardware



## Step 1:

Prepare qubit state by Rabi oscillation

# Schematic of Measurement Setup



$$g \equiv \sqrt{G/2}$$

$h_e, h_f$  effective noise modes

generalization of accessible expectation values:

$$\langle (S_e^\dagger)^n S_f^m \rangle = g^{n+m} \langle (a^\dagger)^n a^m \rangle$$

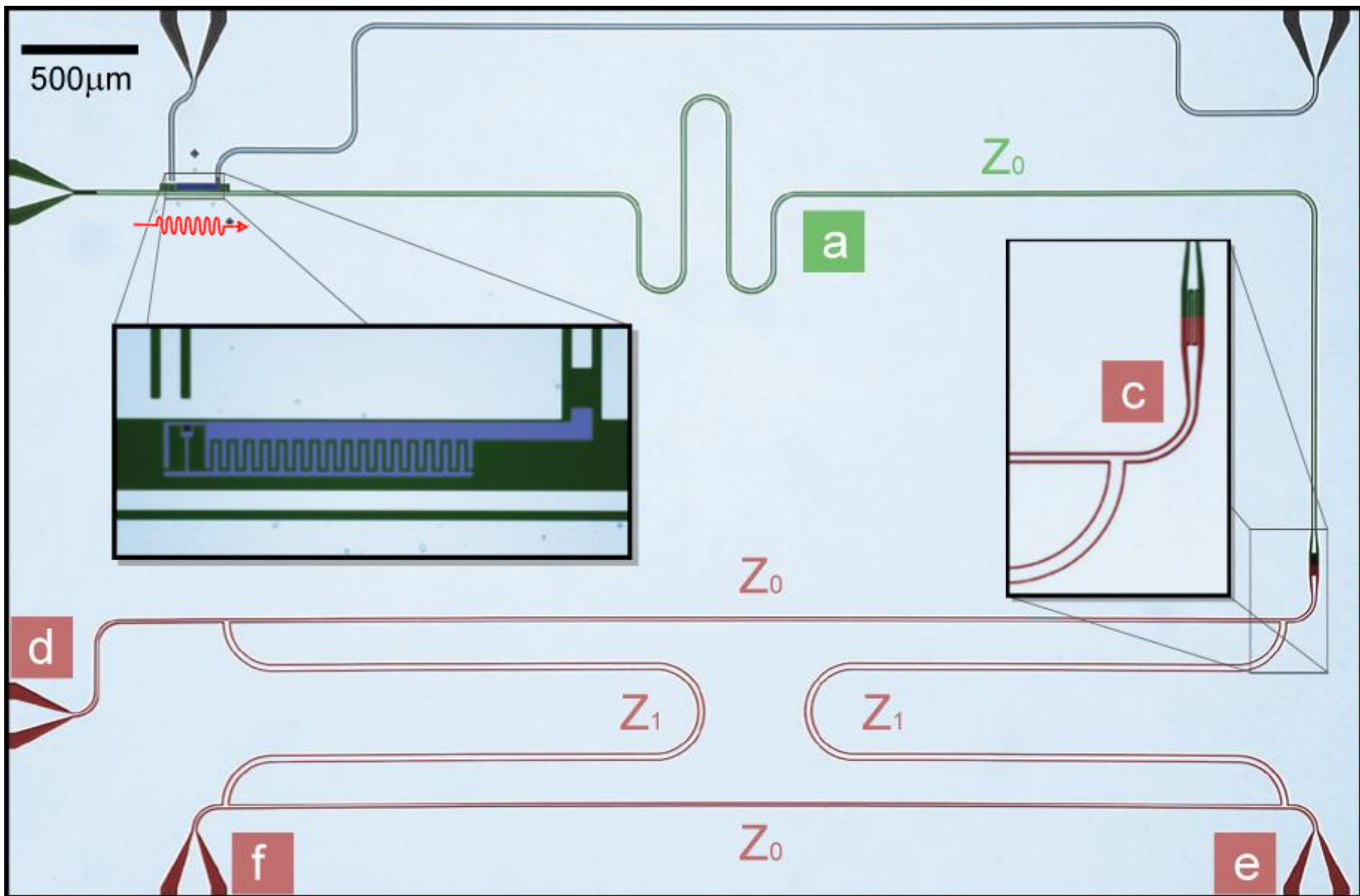
C. Eichler et al., *PRA* **86**, 032106 (2012)

M. P. da Silva et al., *PRA* **82**, 043804 (2010)

D. Bozyigit et al., *Nat. Phys.* **7**, 154 (2011)

G. S. Argawal et al., *PRA* **49**, 2 (1994). S. L. Braunstein et al., *PRA* **43**, 1153 (1991)

# Single Sided Cavity and Beam Splitter

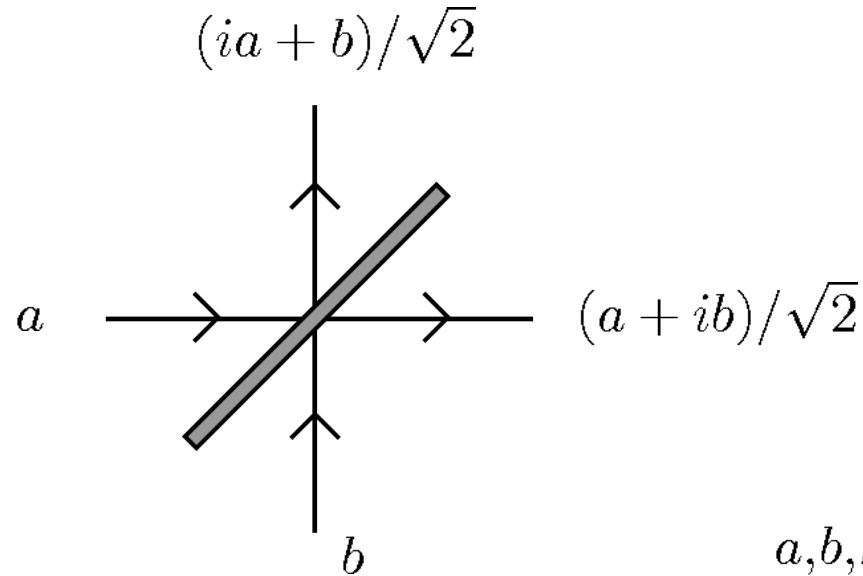






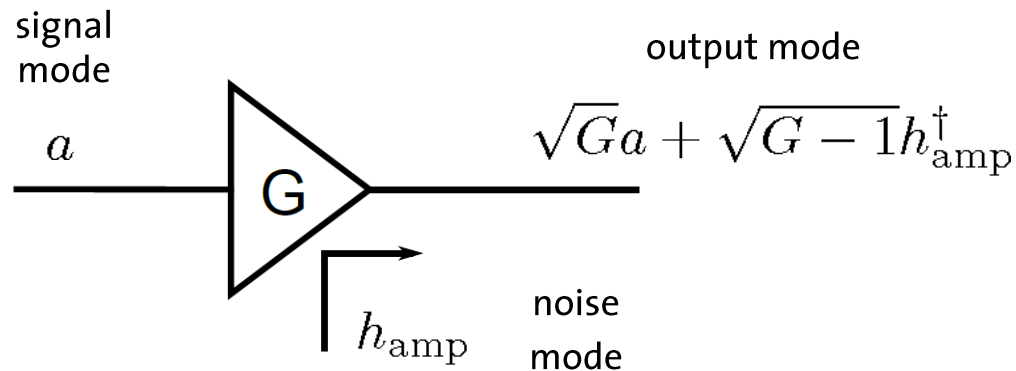
# Detection Scheme using Beam Splitters, Amplifiers ...

beam splitter:



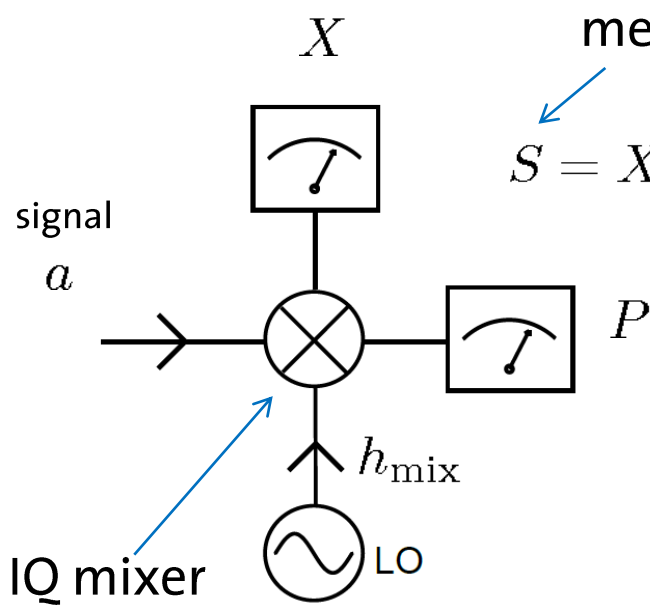
$a, b, h, \dots$  bosonic field operators

linear amplifier:



# ... and Quadrature Detectors

measuring field amplitude instead of photon number:



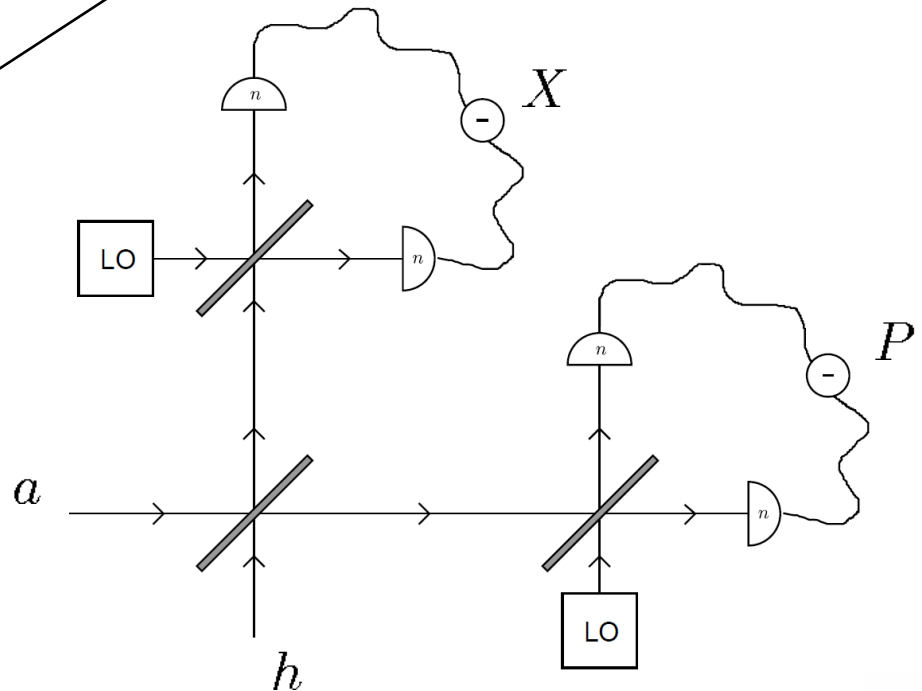
measured observable

$$S = X + iP = a + h_{\text{mix}}^\dagger$$

optical analogue

M. P. da Silva et al.,  
PRA 82, 043804 (2010).

homodyne  
detection  
scheme



# The Signal in One Channel of the Setup

signal mode  $a$  , vacuum mode  $v$

$$\longrightarrow (a + iv)/\sqrt{2}$$

$$\longrightarrow \sqrt{G/2}(a + iv) + \sqrt{G-1}h_{\text{amp}}^\dagger$$

$$\longrightarrow \sqrt{G/2}(a + iv) + \underbrace{\sqrt{G-1}h_{\text{amp}}^\dagger + h_{\text{mix}}^\dagger}_{\propto h^\dagger}$$

$$\equiv \sqrt{G/2}(a + h^\dagger)$$

$$\equiv S = X + iP$$

effective noise mode

Beam splitter

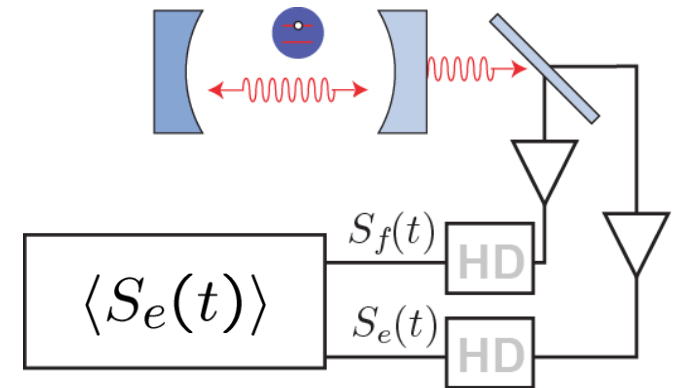
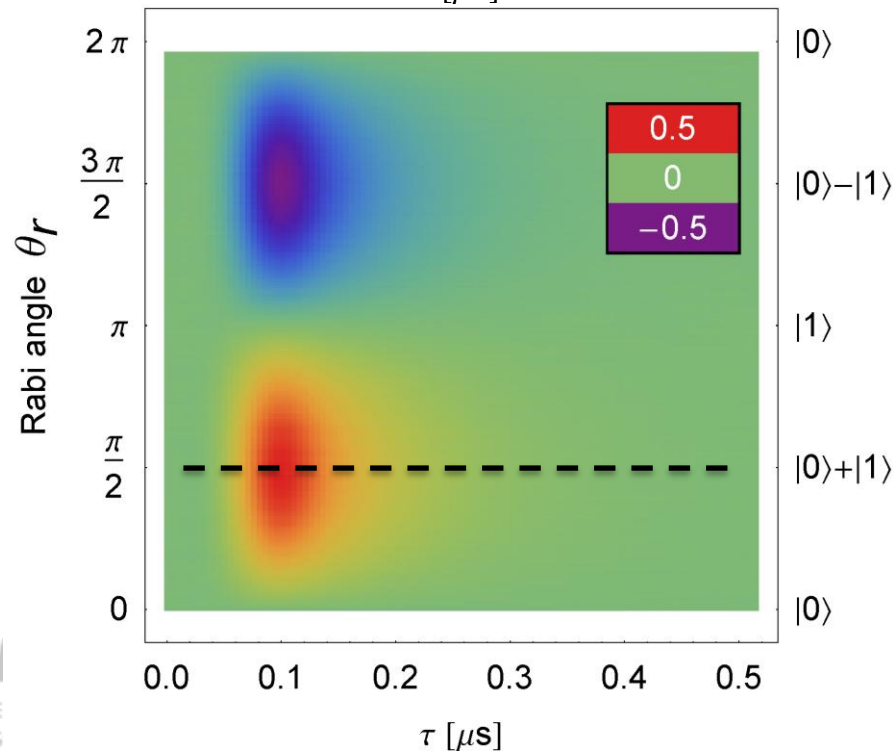
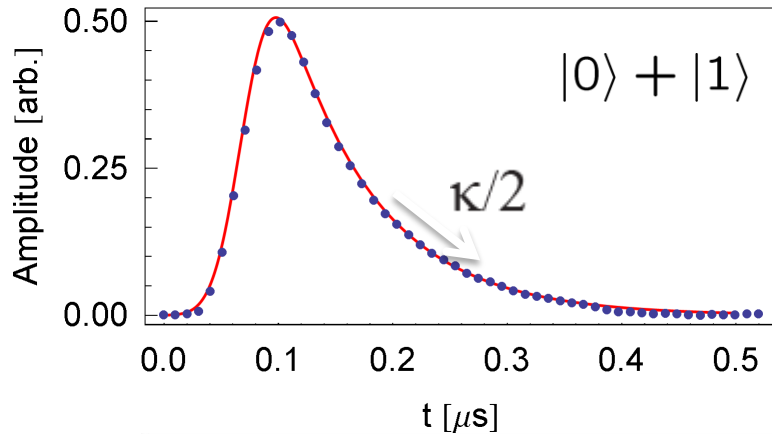
Linear amplifier

Mixer

analogous for second channel!

# Cavity Field Quadrature Measurement

Measure quadratures at channel b:



$$\langle S_e(t) \rangle \propto \langle a(t) \rangle \propto \sin(\theta_r)/2$$

Time-dependence:

- Falling edge: cavity decay
- Rising edge: detection bandwidth

Rabi angle dependence:

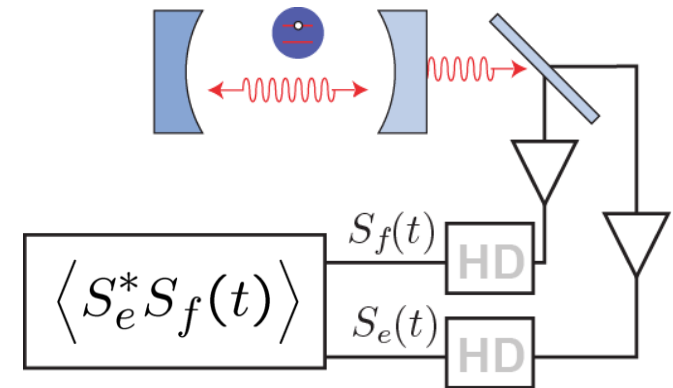
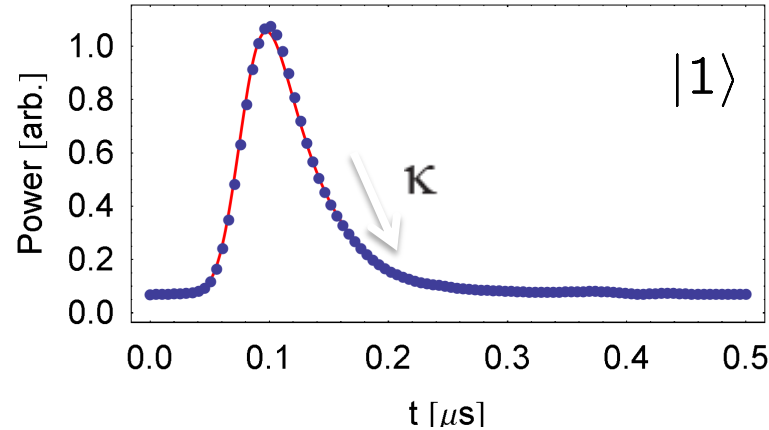
- Maximum signal for  $|0\rangle + |1\rangle$
- No signal for  $|1\rangle$
- Excellent agreement with theory

*D. Bozyigit et al., Nat. Phys. 7, 154 (2011)*

*A. Houck et al., Nature 449, 328 (2007)*

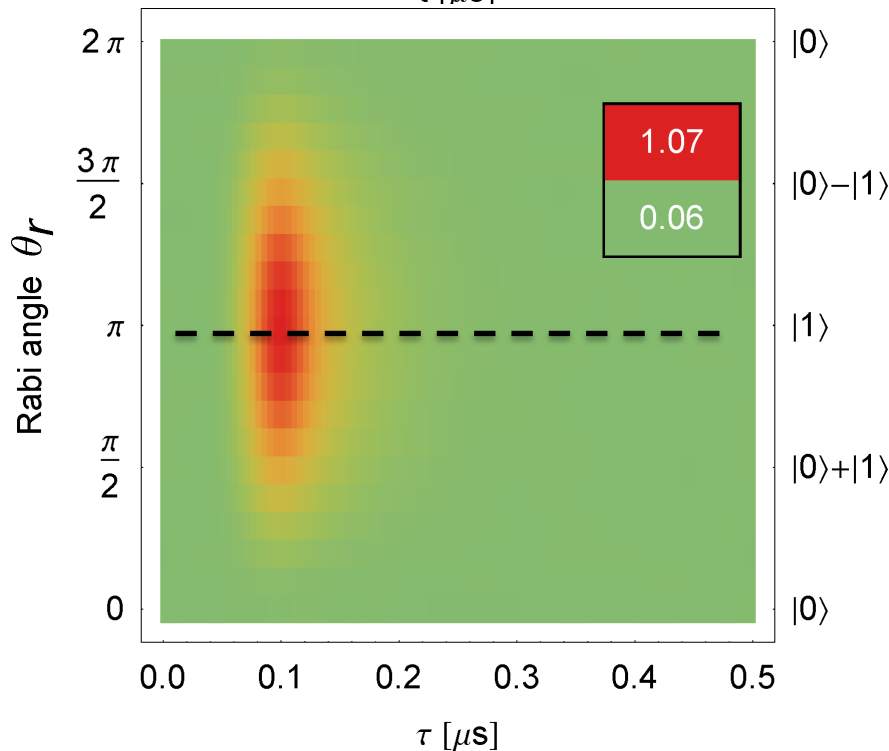
# Cavity Photon Number Measurement

Measure crosspower between channel e&f:



$$\langle S_e^* S_f(t) \rangle \propto \langle a^\dagger(t) a(t) \rangle + N_{ef}$$

$$\propto \sin^2(\theta_r/2)$$



Time-dependence:

- Falling edge: cavity decay
- Rising edge: detection bandwidth

Rabi angle dependence:

- **Maximum signal for  $|1\rangle$**
- Excellent agreement with theory

# Single-Channel Power vs. Two-Channel Cross Power

Single channel power:

$$\langle S_e^\dagger S_e \rangle / g^2 = \langle a^\dagger a \rangle + \langle h_e h_e^\dagger \rangle + \underbrace{\langle a \rangle \langle h_e^\dagger \rangle + \langle a^\dagger \rangle \langle h_e \rangle}_{=0}$$

$\langle a h_e^\dagger \rangle = \langle a \rangle \langle h_e^\dagger \rangle$   
 system noise uncorrelated from signal  
 signal photons  
 added noise photons  
 system noise is Gaussian with vanishing mean

... vs. cross power:

$$\langle S_e^\dagger S_f \rangle / g^2 = \langle a^\dagger a \rangle + \underbrace{\langle h_e h_f^\dagger \rangle}_{=0} + \underbrace{\langle a \rangle \langle h_e^\dagger \rangle + \langle a^\dagger \rangle \langle h_e \rangle}_{=0} = \langle a^\dagger a \rangle$$

$v$  in vacuum  
 Noise in 2 detection channels uncorrelated

... similar for higher order moments:

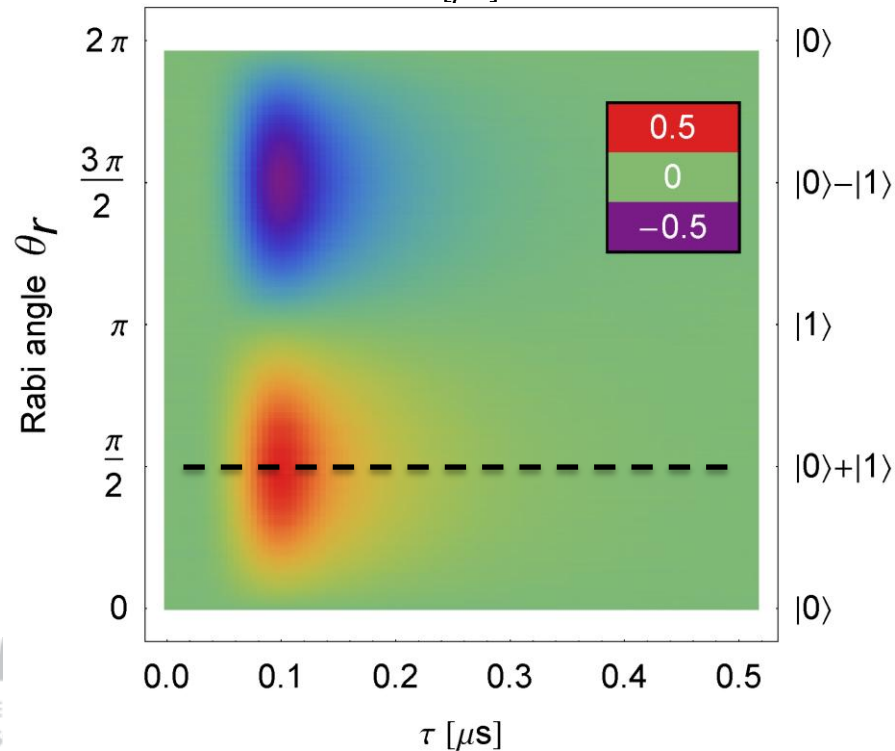
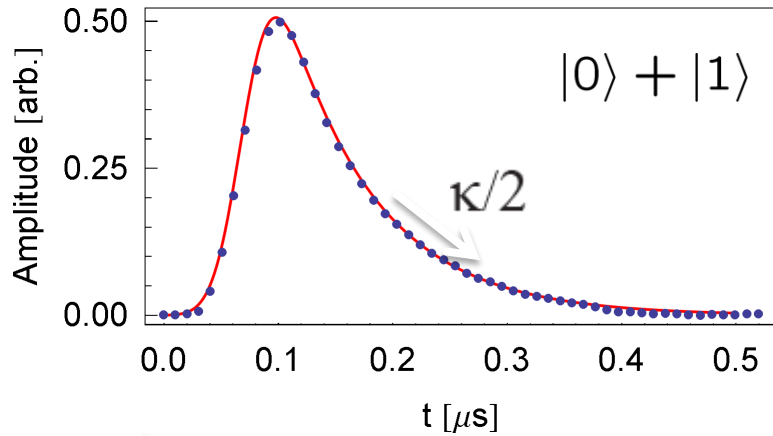
$$\langle (S_e^\dagger)^2 S_f^2 \rangle = \langle (a^\dagger)^2 a^2 \rangle$$

whereas

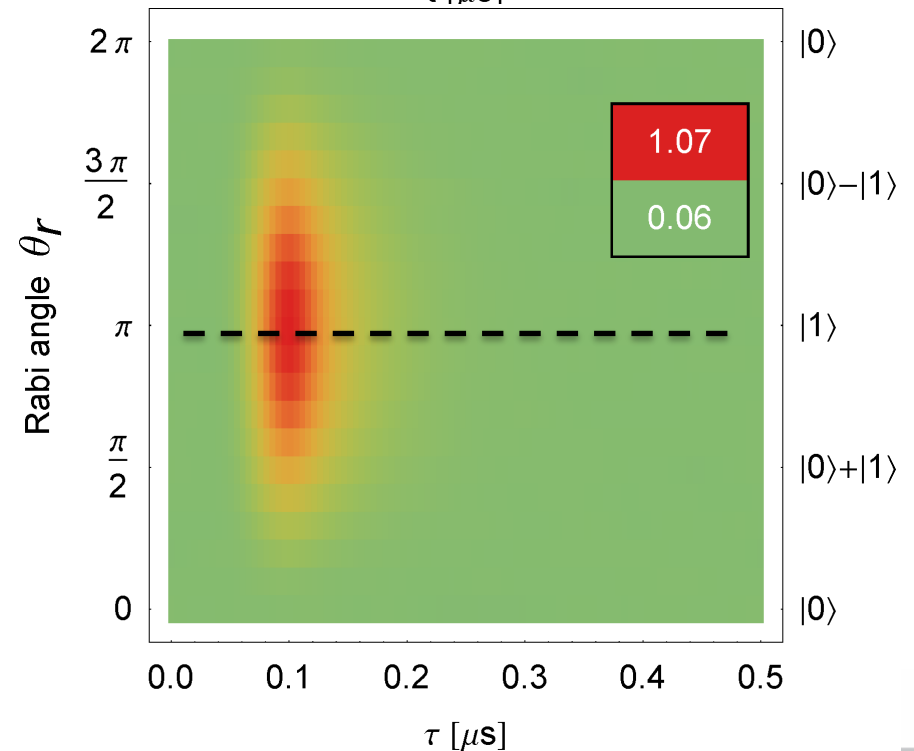
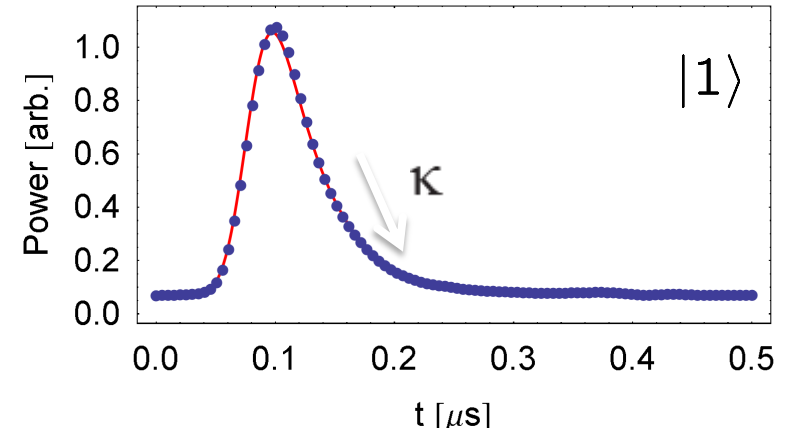
$$\langle S_e^\dagger S_e S_f^\dagger S_f \rangle = \langle (a^\dagger)^2 a^2 \rangle + \langle a^\dagger a \rangle \langle h_e h_e^\dagger \rangle + \dots$$

# Field Quadrature and Photon Number Measurements

Measure quadratures at channel b:



Measure cross-power between channel e&f:

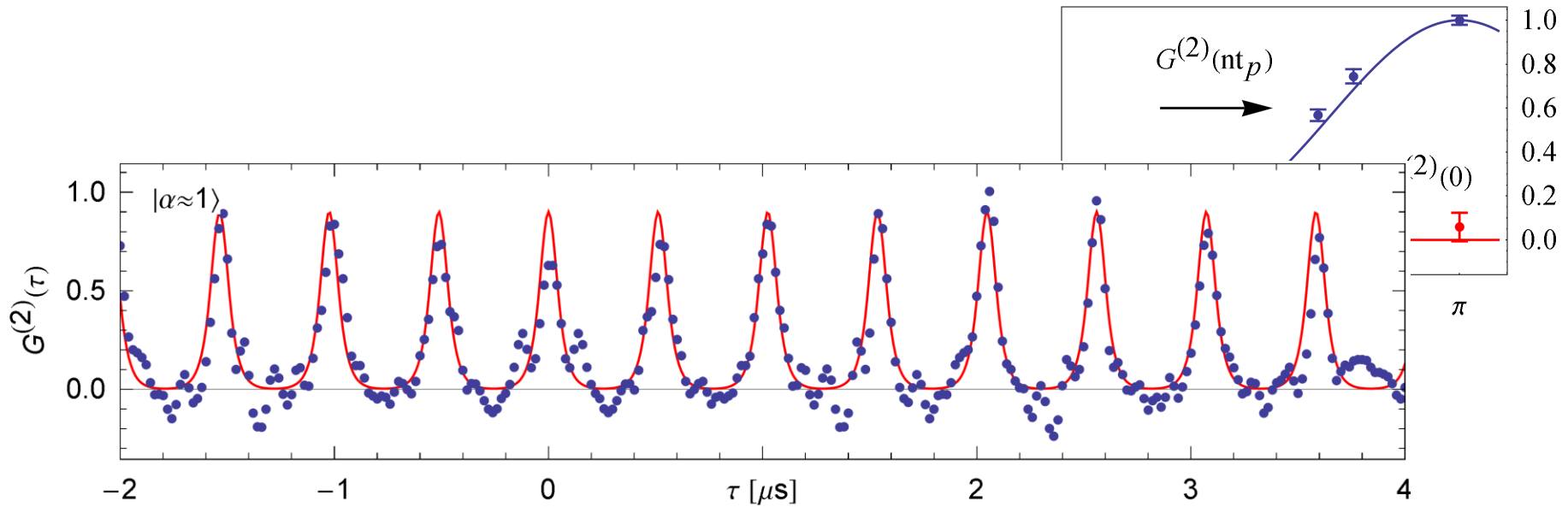
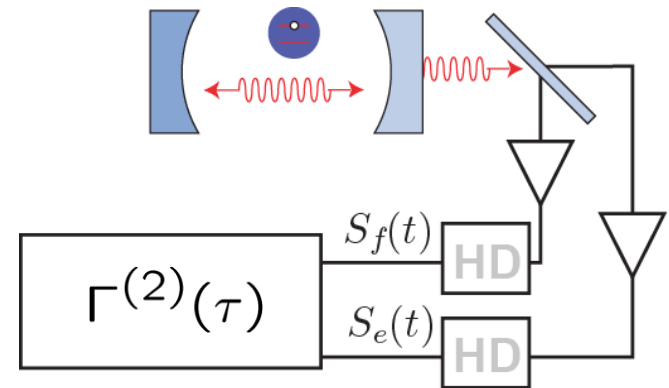


# $G^{(2)}$ Measurement

Measure power correlation between channel e & f:

$$\Gamma^{(2)}(\tau) = \int \langle S_e^*(t) S_e^* S_f(t + \tau) S_f(t) \rangle dt$$

$$G^{(2)}(\tau) = \Gamma_{prep}^{(2)}(\tau) - \Gamma_{ss}^{(2)}(\tau)$$



$G^{(2)}$  measurement for a microwave frequency single photon source

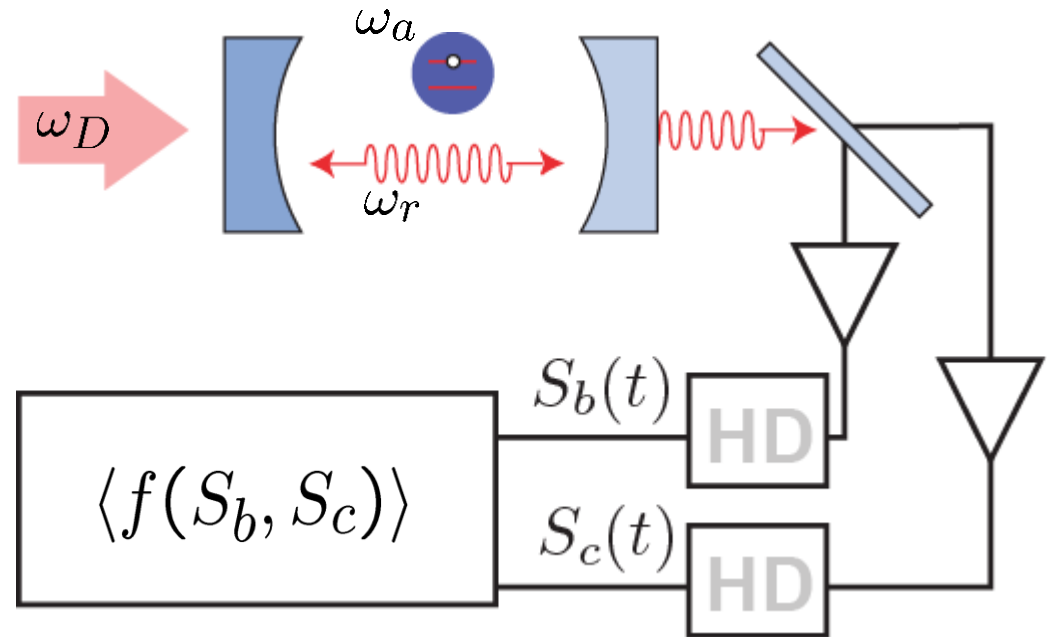


---

# Continuously Pumped Single Photon Source and Beam-Splitter

# Continuously Pumped Microwave Single Photon Source

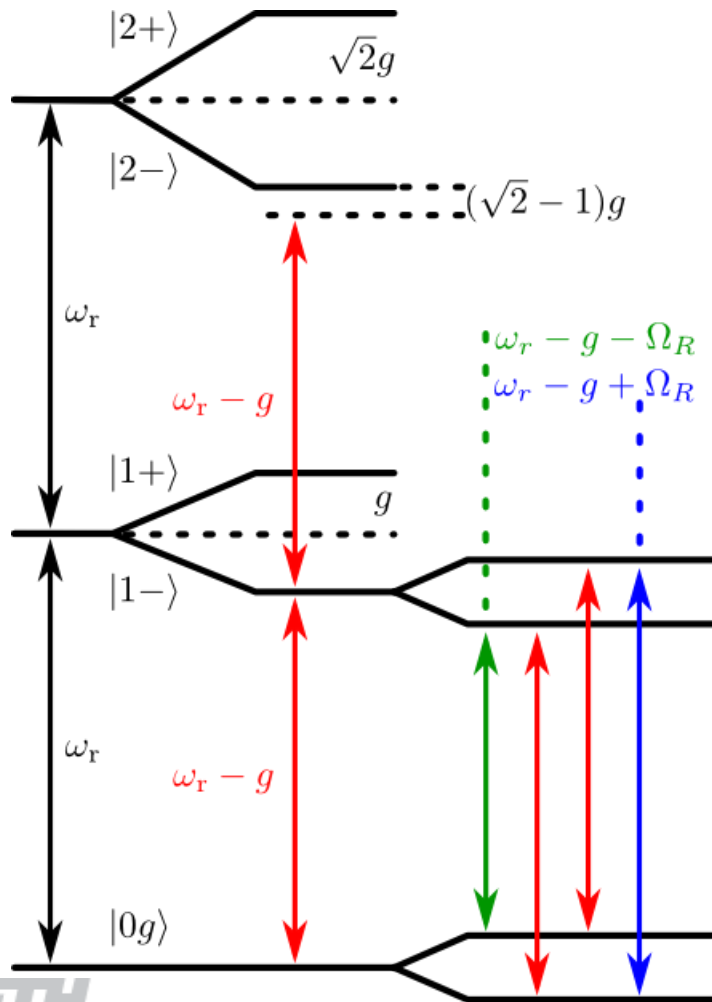
- Based on photon blockade (c.f. Coulomb blockade)  
Imamoglu et al., PRL 79, 1467 (1997)
- mediated photon/photon interactions
- Characterization by field amplitude measurements
- FPGA based correlation analysis



M. P. da Silva et al., PRA 82, 043804 (2010)  
D. Bozyigit et al., Nat. Phys. 7, 154 (2011)  
C. Lang et al., PRL 106, 243601 (2011)

# Photon Blockade: A Single Photon Turnstile

Level diagram:



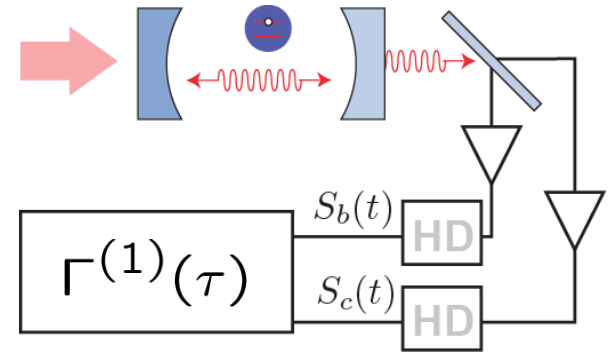
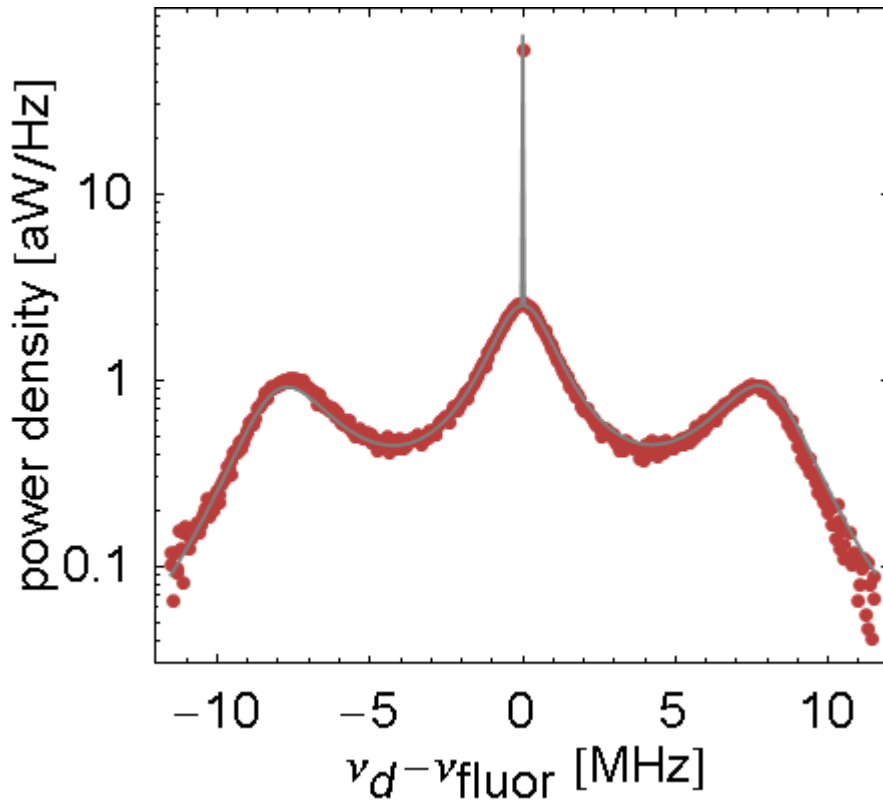
- Vacuum Rabi mode splitting:  
 $|n, \mp\rangle = 1/\sqrt{2} \cdot (|n, g\rangle \mp |n-1, e\rangle)$
- Drive:  
 $\omega_p = \omega_r - g$
- Photon blockade: first photon enters cavity second is blocked
- mediated photon/photon interactions
- Effective two-level system (polariton)  
 $|\downarrow\rangle = |0, g\rangle \quad |\uparrow\rangle = |1, -\rangle$
- Mollow-type triplet:

$$\omega_{1,2,3} = \omega_p \begin{cases} +0 \\ \pm\Omega_R \end{cases}$$

# Polariton Mollow Triplet Measurement

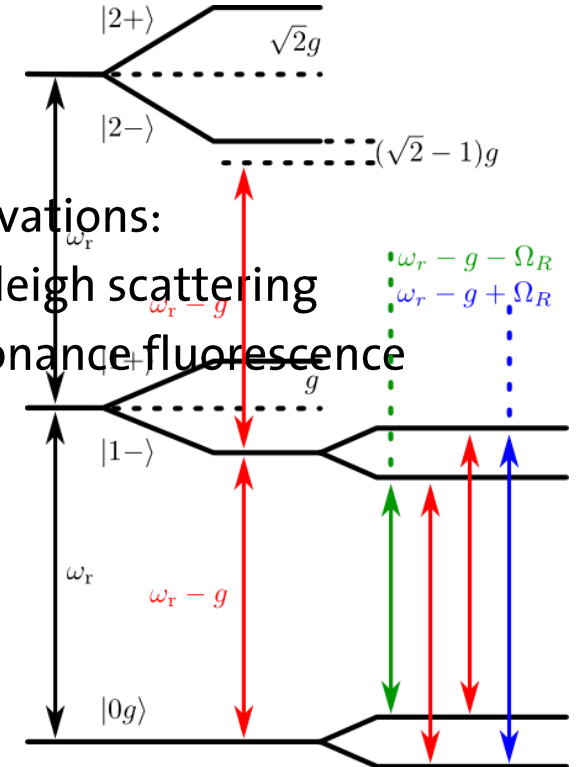
(cross-)power spectrum:

$$\mathcal{F}\{\Gamma^{(1)}(\tau)\} = \langle \mathcal{F}\{S_b(t)\} \cdot \mathcal{F}\{S_c(t)\}^* \rangle$$

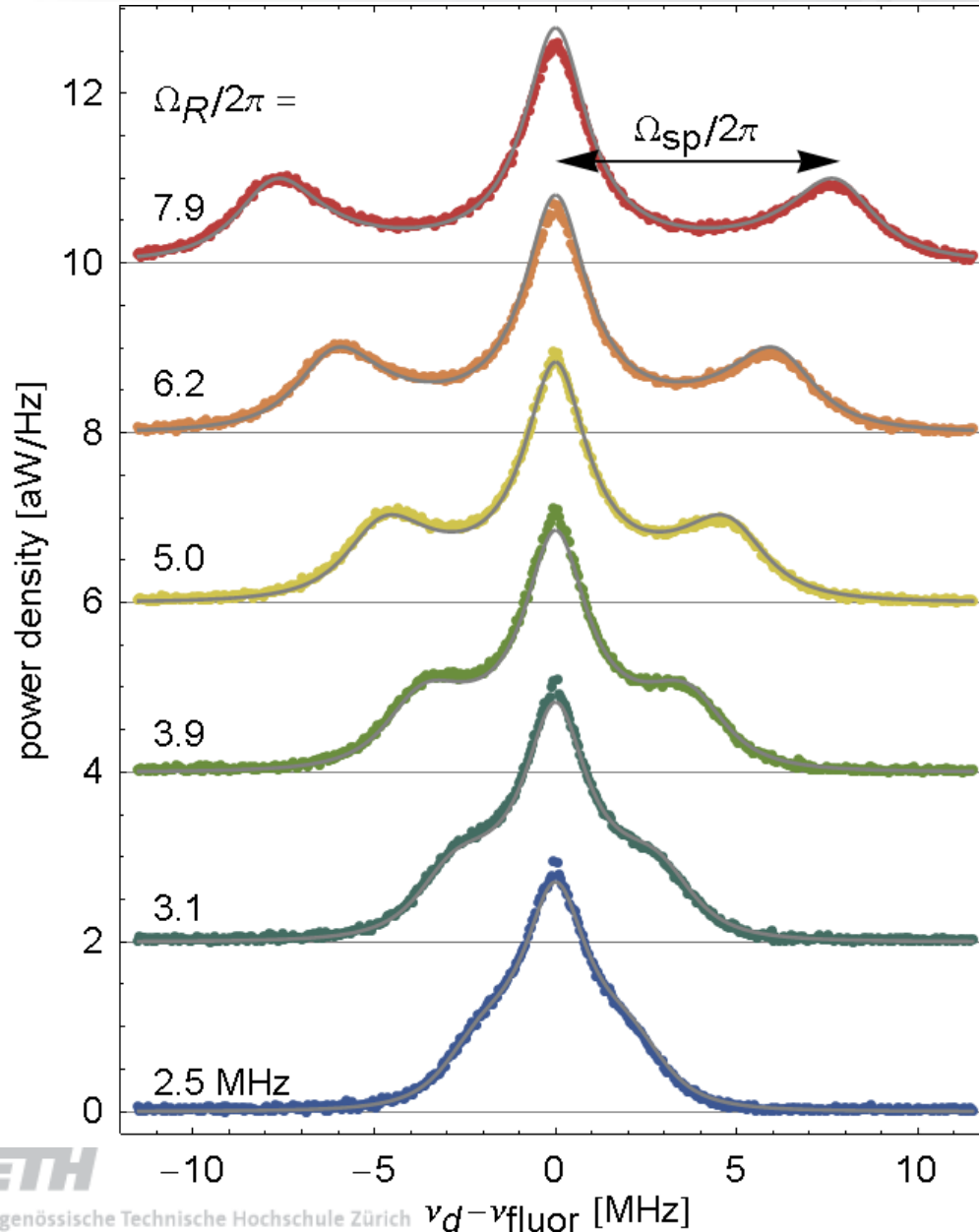


observations:

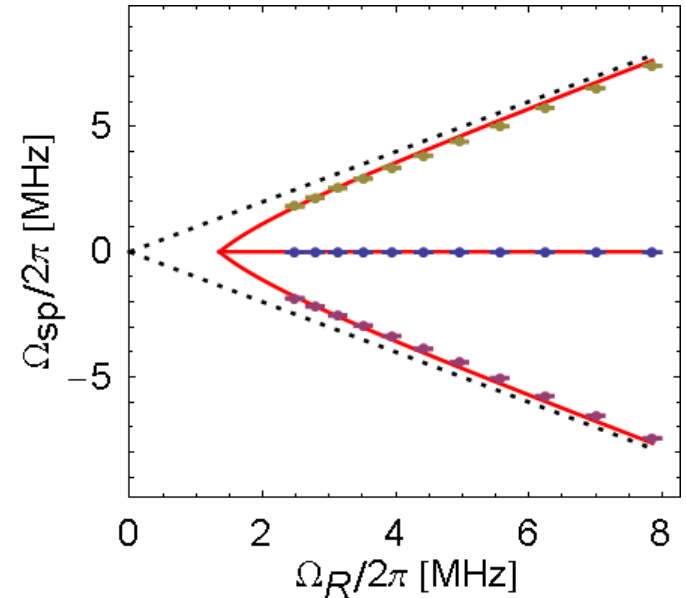
- Rayleigh scattering
- resonance fluorescence



# Dependence on Drive Amplitude



- ‘Mollow’ fluorescence sidebands at Rabi frequency  $\Omega_{sp}$

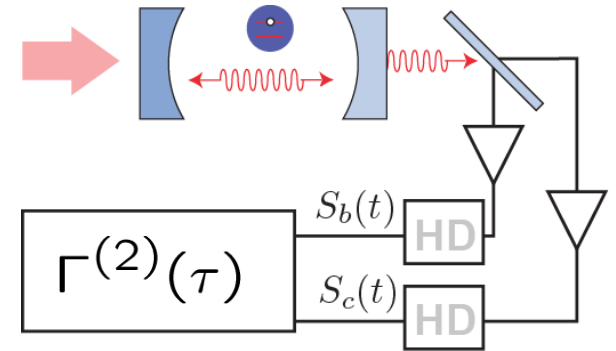
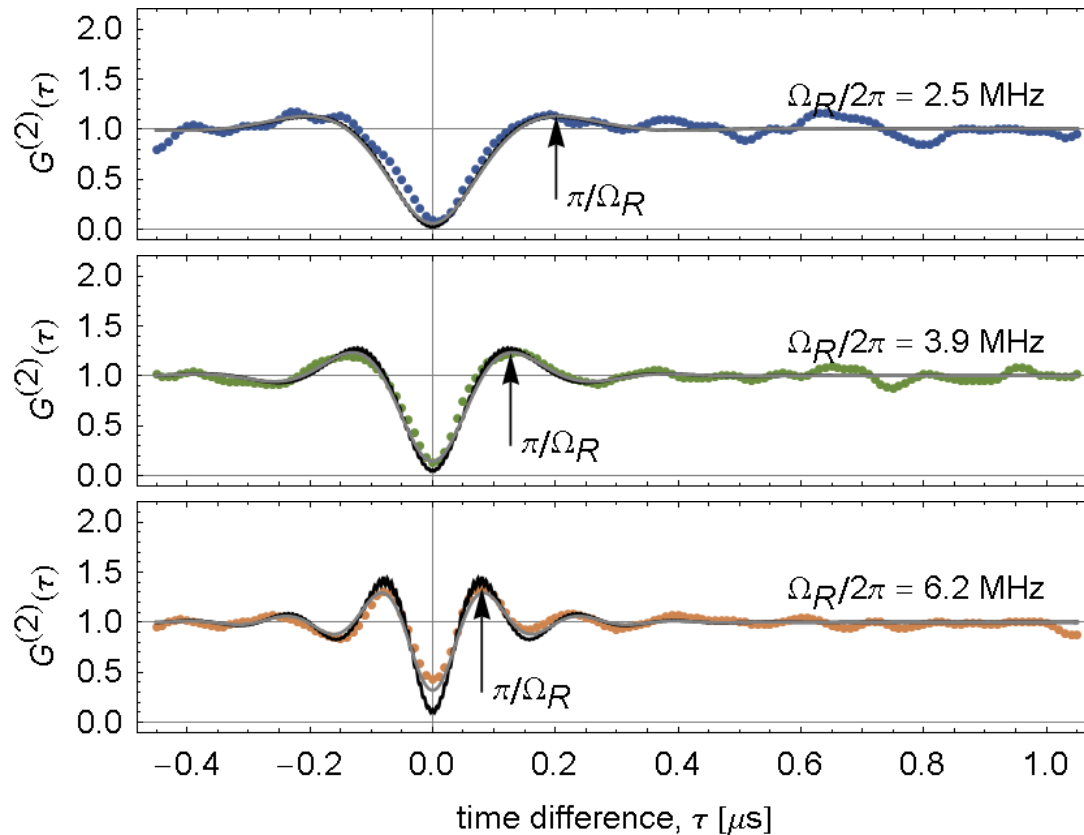


- analytical expression explains nonlinear drive scaling

# Antibunching and Subpoissonian Statistics

- intensity/intensity correlation function (dots)

$$\Gamma^{(2)}(\tau) = \int \langle S_b^* S_b(t) S_c^* S_c(t + \tau) \rangle dt$$



observations:

- sub-Poissonian statistics
- anti-correlation at  $\tau = 0$
- Rabi oscillations visible

solid lines are master equation simulations

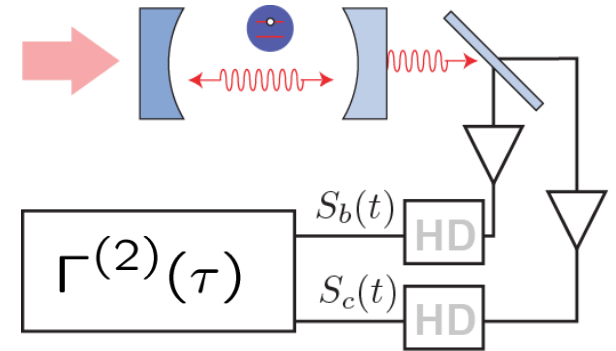
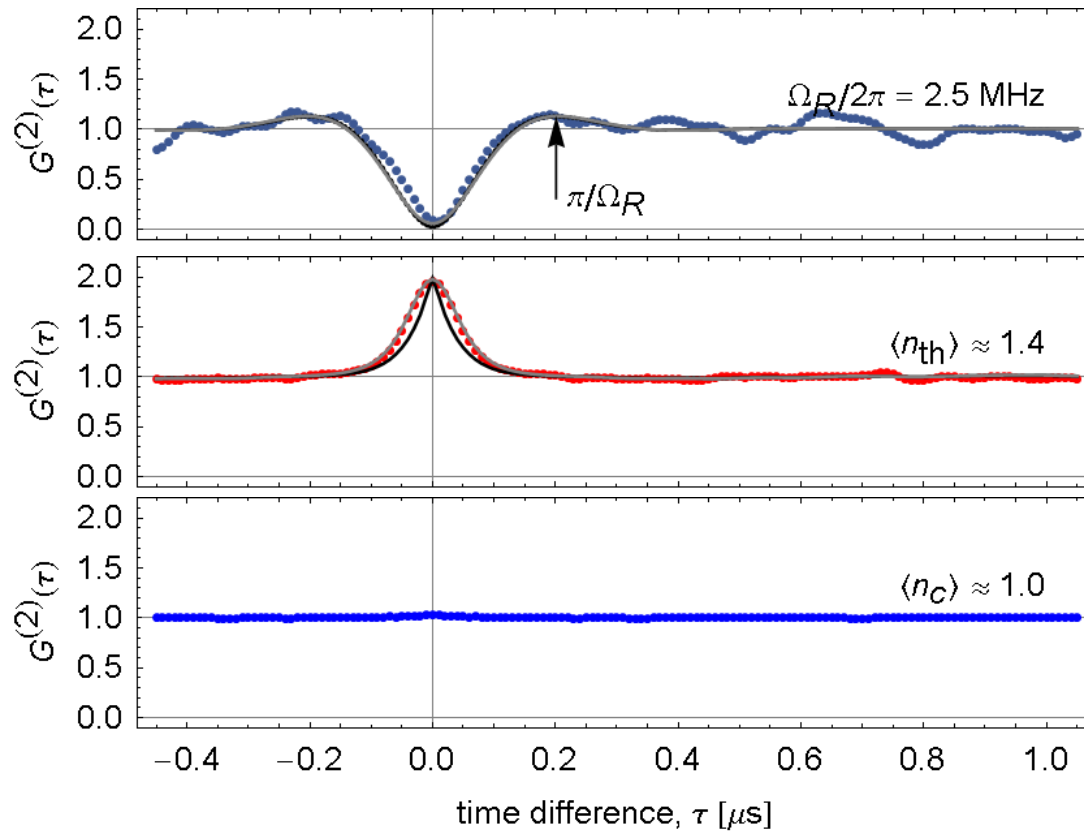
C. Lang *et al.*, *PRL* 106, 243601 (2011)

also dispersive photon blockade: A. J. Hoffman *et al.*, *PRL* 107, 053602 (2011)

# Compare to Thermal and Coherent Fields

- intensity/intensity correlation function (dots)

$$\Gamma^{(2)}(\tau) = \int \langle S_b^* S_b(t) S_c^* S_c(t + \tau) \rangle dt$$



thermal field:

- $G^{(2)}(0) = 2$
- $G^{(2)}(\tau) = 1$  for large  $\tau$

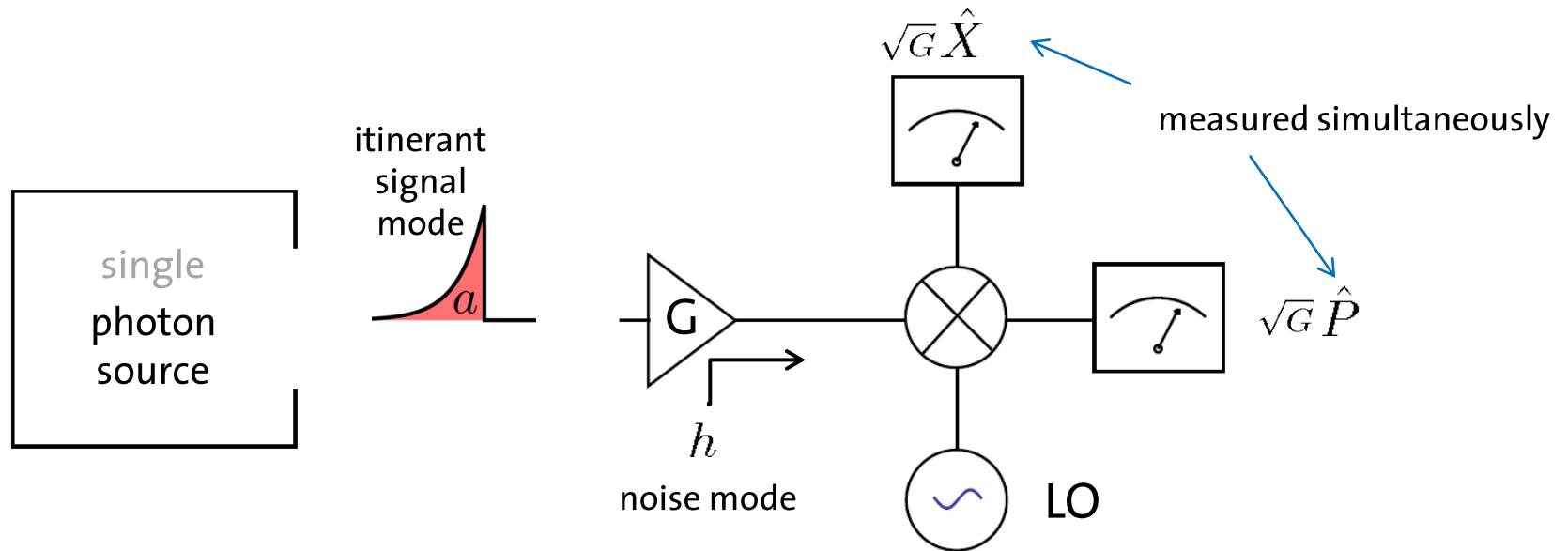
coherent field:

- $G^{(2)} = 1$

# Tomography of Pulsed Single Photon Source



# Tomography using Microwave Quadrature Detection



complex amplitude:  $\sqrt{G}(a + h^\dagger) \equiv \hat{S} \equiv \sqrt{G}(\hat{X} + i\hat{P})$

ideal (quantum limited) case:  $h$  in vacuum state  $|0\rangle$

real (commercial amplifier) case:  $h$  in thermal state with  $N_{\text{noise}}$  photons

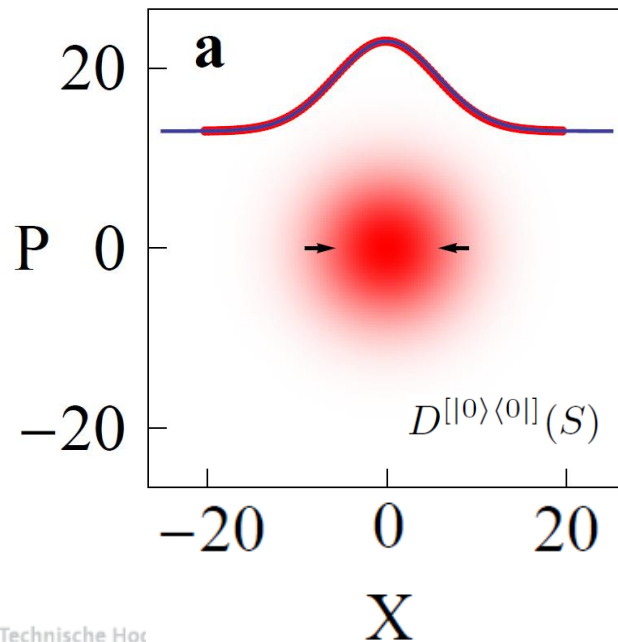
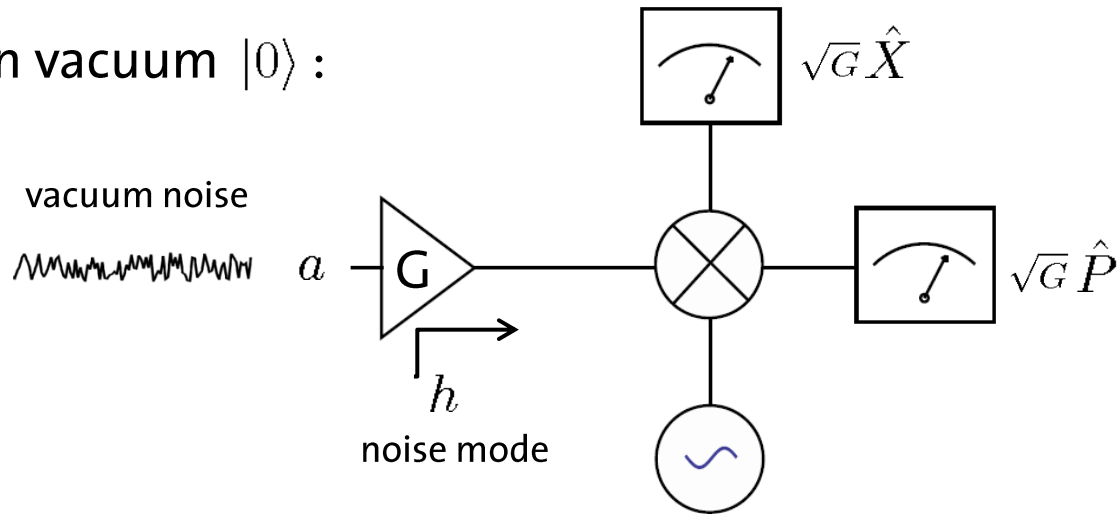
C. Eichler et al., *PRA* **86**, 032106 (2012)

M. P. da Silva et al., *PRA* **82**, 043804 (2010)

C. M. Caves, *PRD* **26**, 1817 (1982)

# Full Tomography of a Single Propagating Mode

1) prepare  $a$  in vacuum  $|0\rangle$  :



← record histogram  $D^{[|0\rangle\langle 0|]}(S)$   
of measurement results  $S/\sqrt{G} = X + iP$

→ normal distribution with variance

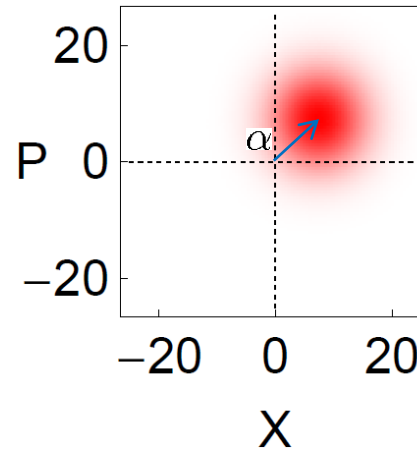
$$2\sigma^2 = \langle \hat{S}^\dagger \hat{S} \rangle / G = \frac{1}{G} \int d^2 S D^{[|0\rangle\langle 0|]}(S) S^* S = 67$$

$h$  introduces thermal noise  
with mean photon number  $N_{\text{noise}}$

# Coherent State Histograms

2) prepare  $a$  in coherent state  $|\alpha\rangle$  :

MW generator



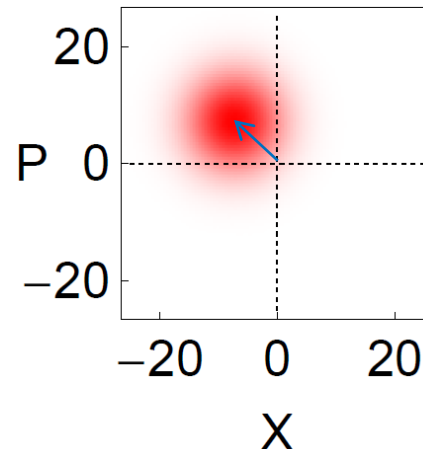
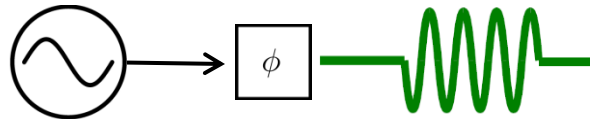
$$|\alpha| \approx 6.3$$

$$\Leftrightarrow$$

$$\langle a^\dagger a \rangle \approx 41 \sim N_{\text{noise}}$$

3) rotate phase  $|e^{i\phi}\alpha\rangle$  :

MW generator



Question: What can we learn about state when  $\langle a^\dagger a \rangle \leq 1$  ?

# Single Photon Source Histogram

store 2D histogram  $D^{[\rho]}(S)$  from  $S/\sqrt{G} = X + iP$  measurement results:

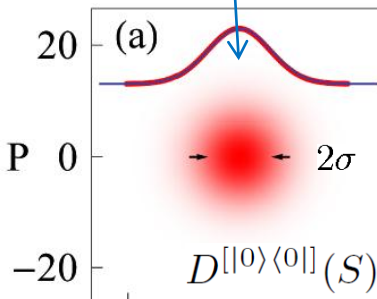
corresponding phase space distribution

signal mode  $a$   
in vacuum

Q - function  
of noise mode :

$$Q_h$$

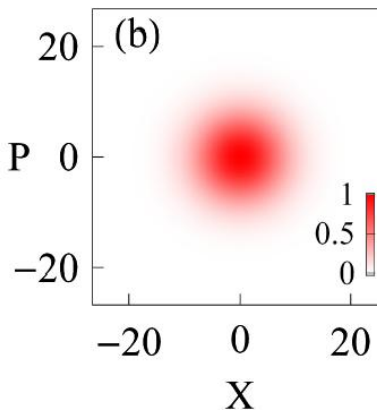
← P



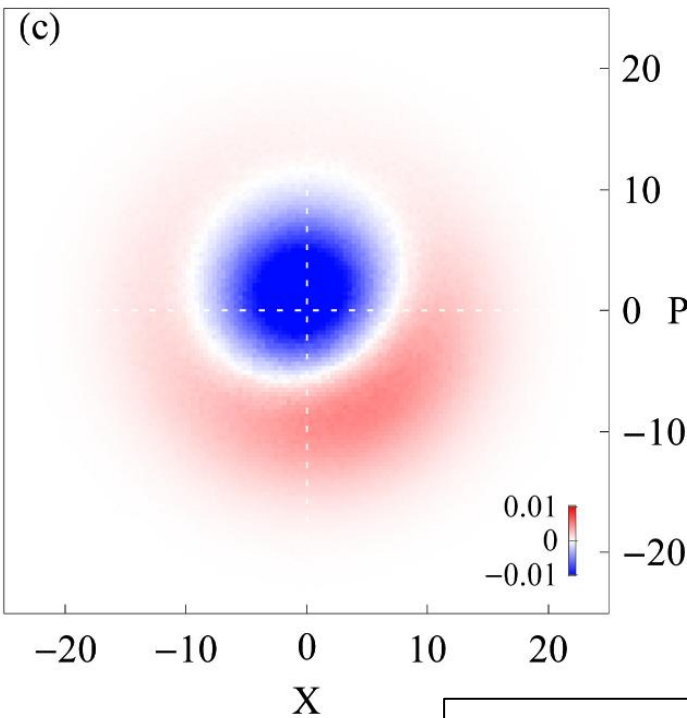
convolution  
with P - function  
of signal

$$Q_h * P_a$$

← P



signal mode  $a$   
in single photon  
Fock state



separate noise  $h$  from  
signal  $a$  systematically!

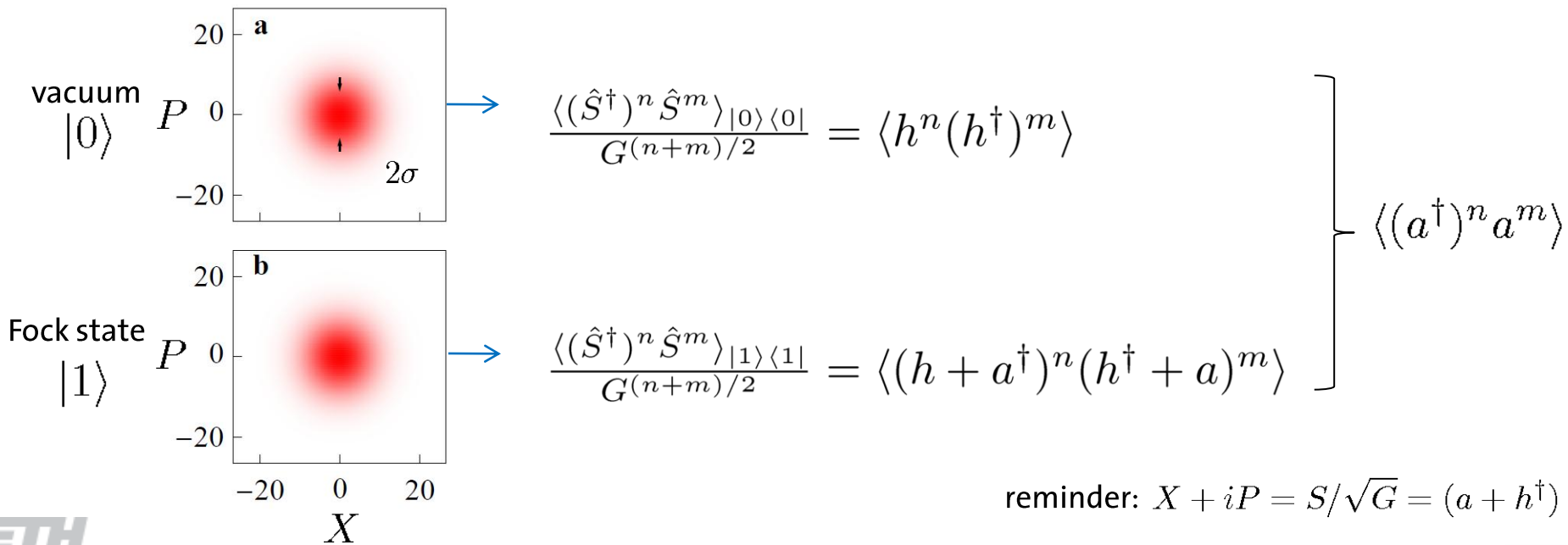
# Statistical Analysis of Histograms

systematic mode separation:

histogram moments: 
$$\langle (\hat{S}^\dagger)^n \hat{S}^m \rangle_\rho = \int d^2 S (S^*)^n S^m D^{[\rho]}(S)$$

1. calculate histogram moments

2. algebraic inversion

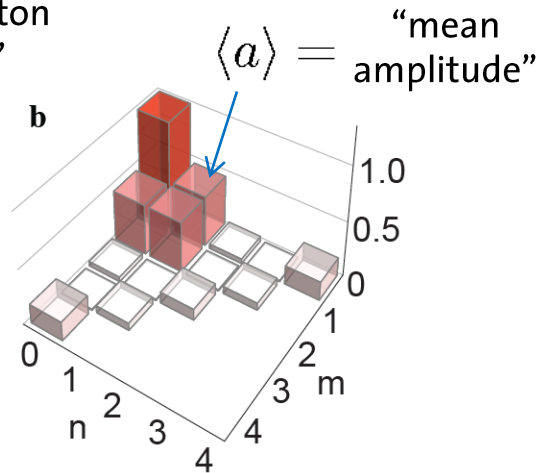
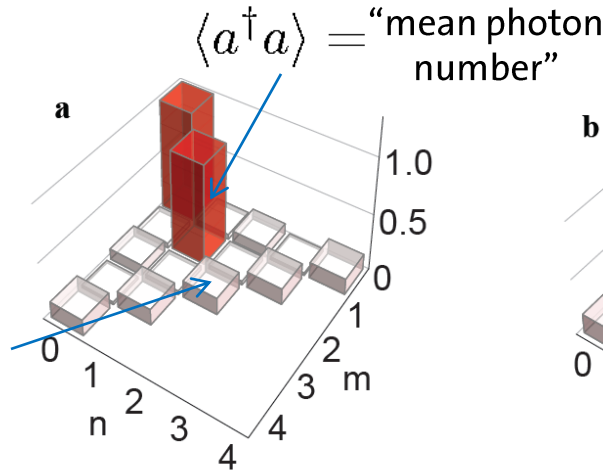


# State Dependent Moments of Probability Distribution

moments  $|\langle (a^\dagger)^n a^m \rangle|$  for different prepared states:

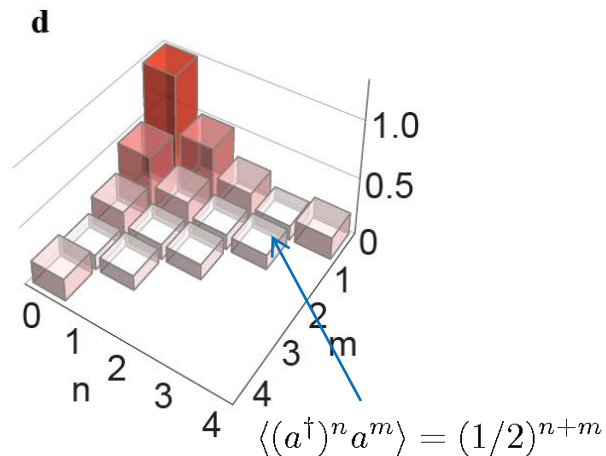
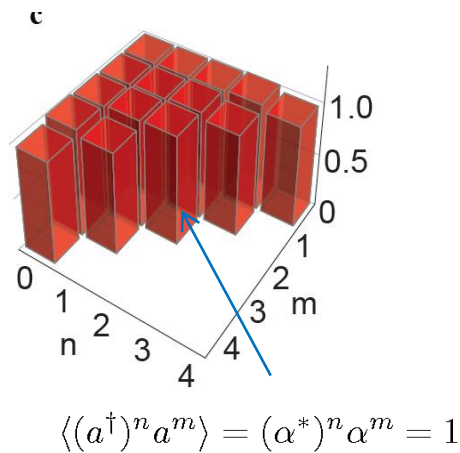
Fock state  
 $|1\rangle$

$\langle (a^\dagger)^2 a^2 \rangle \approx 0$   
“anti bunching”



superposition  
 $\frac{1}{\sqrt{2}}(|0\rangle + e^{i\phi}|1\rangle)$

coherent state  
 $|\alpha = 1\rangle$

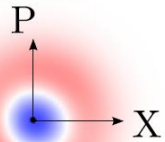
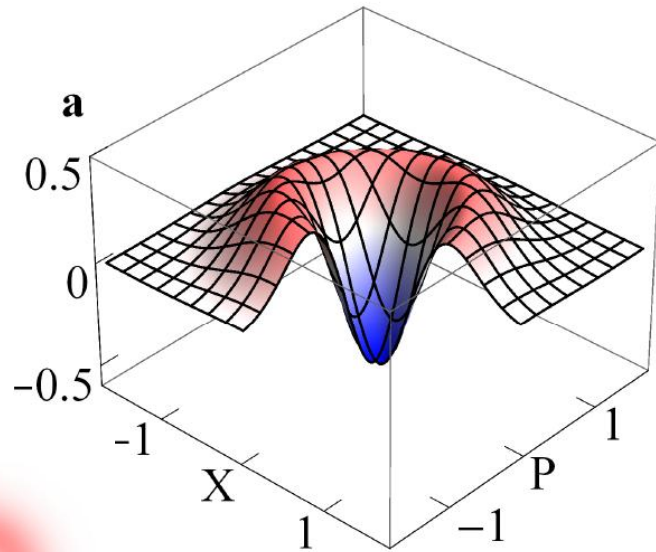


coherent state  
 $|\alpha = 0.5\rangle$

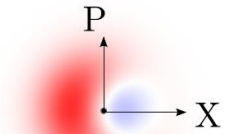
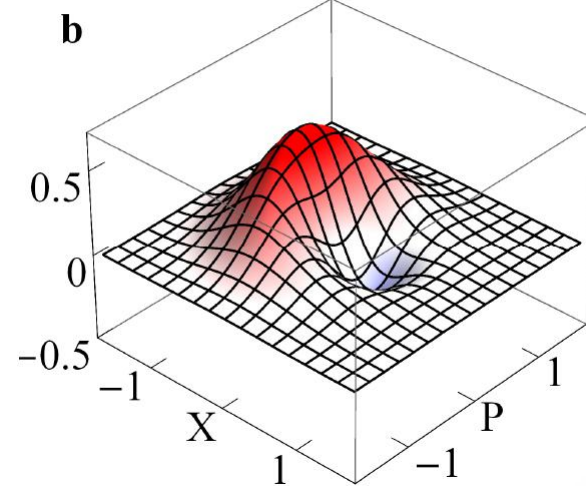
# Reconstructed Wigner Function of Itinerant Photon

Wigner function reconstructed from measured moments:

$$W(\alpha) = \sum_{n,m} \int d^2\lambda \frac{\langle (a^\dagger)^n a^m \rangle (-\lambda^*)^m \lambda^n}{\pi^2 n! m!} e^{(-1/2)|\lambda|^2 + \alpha\lambda^* - \alpha^*\lambda} \quad \text{with} \quad n + m < 4$$



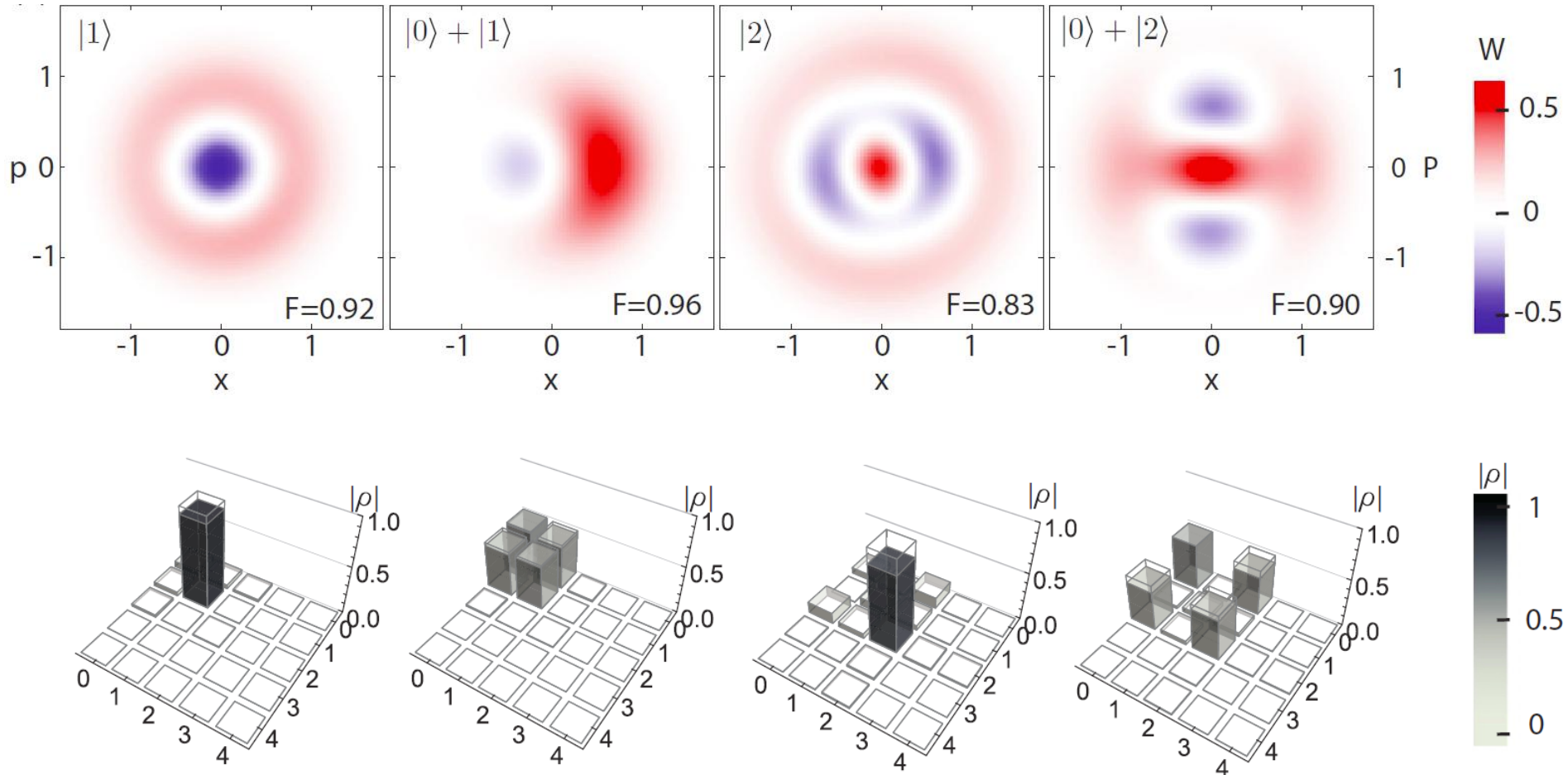
Fock state  
 $|1\rangle$



superposition  
 $\frac{1}{\sqrt{2}}(|0\rangle + e^{i\phi}|1\rangle)$

# Wigner Function and Density Matrices ...

... for propagating multi-photon Fock states and their superpositions:



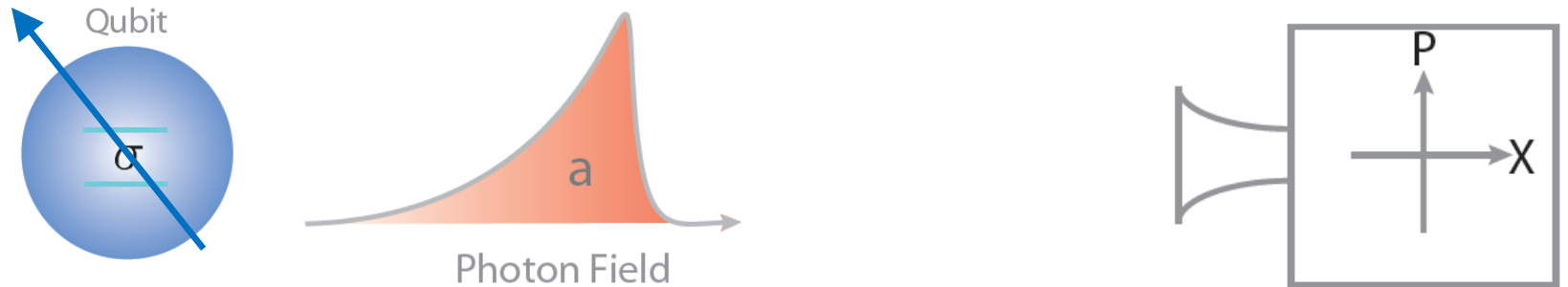
measured using near-quantum-limited parametric amplifier



# Two-Mode Squeezing with Parametric Amplifier

# Entanglement between Propagating Photon and Stationary Qubit

# Entanglement of Localized and Propagating Modes



- test of correlations between propagating photon and qubit
- probe non-local aspects of quantum mechanics in circuits
- interfacing stationary and flying qubits
- entanglement distribution in a quantum network

# Photon/Qubit Entanglement at Optical Frequencies



## Atom–Photon Entanglement

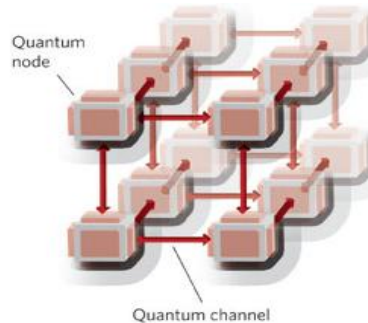
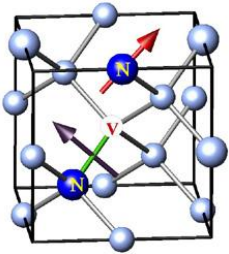
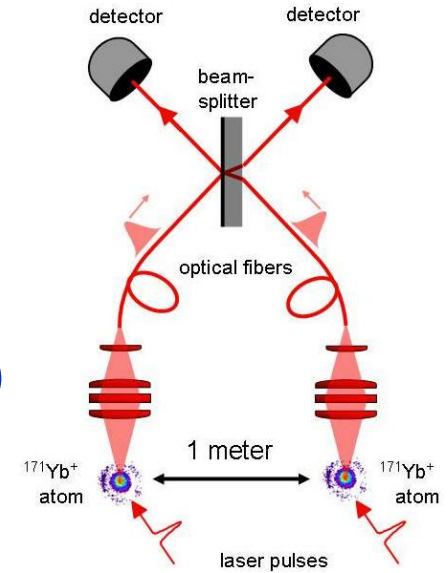
Blinov *et al.*, *Nature* 428, 153 (2004)

Volz *et al.*, *PRL* 96, 030404 (2006)

## Atom–Atom Entanglement

Moehring *et al.*, *Nature* 449, 68 (2007)

Ritter *et al.*, *Nature* 484, 195 (2012)



## The quantum internet

Kimble, *Nature* 453, 1023 (2008)

## Spin–Photon Entanglement

Togan *et al.*, *Nature* 466, 730 (2010)

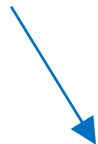
What about superconducting circuits?

# Experiments at Microwave Frequencies

## On-chip entanglement:

- Three Qubits (GHZ, W, Teleportation)
  - DiCarlo *et al.*, *Nature* **467**, 574 (2010)
  - Neely *et al.*, *Nature* **467**, 570 (2010)
  - Baur *et al.*, *PRL* **108**, 040502 (2012)
  - Mlynek *et al.*, arXiv:1202.5191 (2012)
- Qubit- Resonator (arb. Res. states)
  - Haroche /Raimond, *Expl. the Quantum*
  - Hofheinz *et al.*, *Nature* **454**, 310 (2008)
- Res-Res (Noon States)
  - Wang *et al.*, *PRL* **106**, 060401 (2011)
  - Mariani *et al.*, *Nat. Phys.* **7**, 287 (2011)

...



## Itinerant microwave fields:

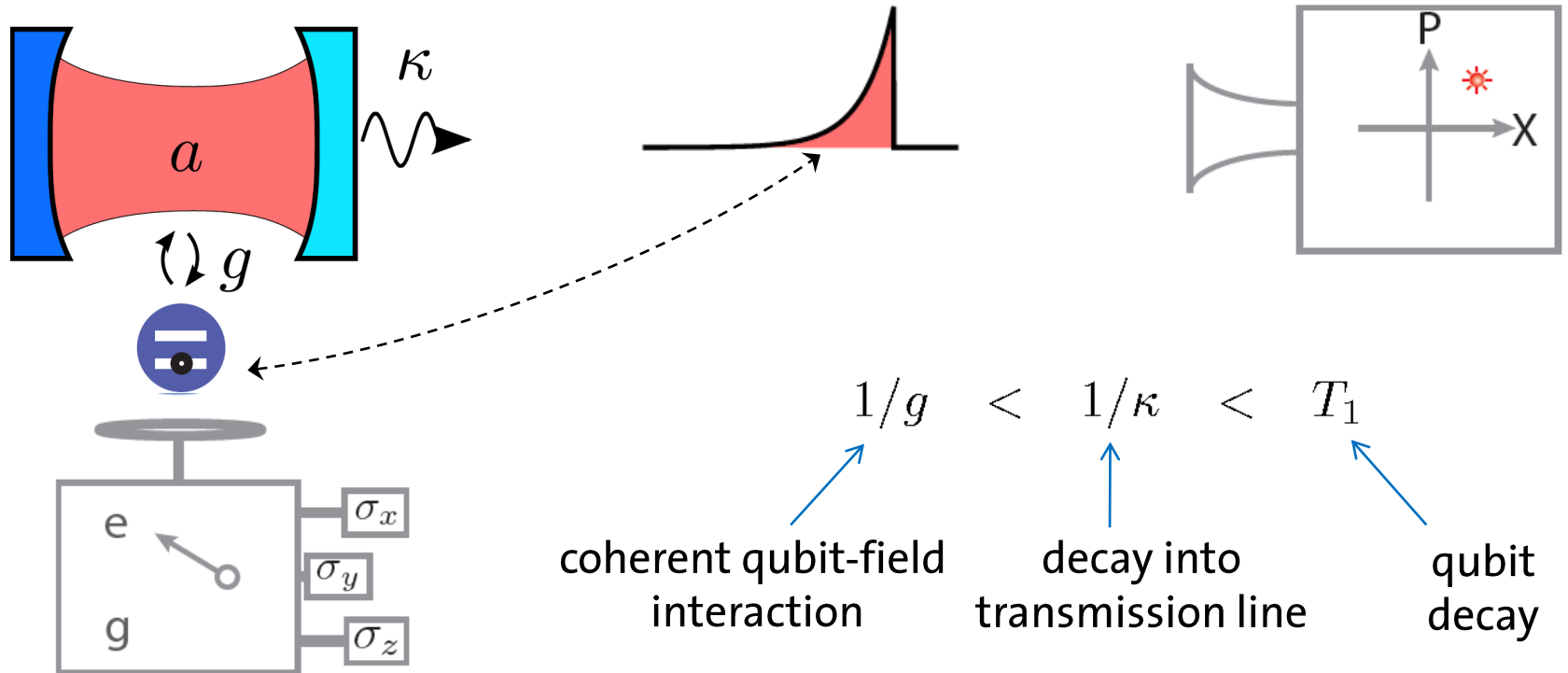
- Single Photons
  - Houck *et al.*, *Nature* **449**, 328 (2007)
  - Bozyigit *et al.*, *Nat. Phys.* **7**, 154 (2011)
  - Eichler *et al.*, *PRL* **106**, 220503 (2011)
  - Lang *et al.*, *PRL* **107**, 073601 (2011)
- Squeezed States/EPR states
  - Castellanos *et al.*, *Nat. Phys.* **4**, 929 (2008)
  - Mallet *et al.*, *PRL* **106**, 220502 (2011)
  - Eichler *et al.*, *PRL* **107**, 113601 (2011)
  - Bergeal *et al.*, *PRL* **108**, 123902 (2012)
  - Flurin *et al.*, arXiv:1204.0732 (2012)

...



Here: Entanglement of stationary qubit with itinerant microwave field.

# Concept of Photon/Qubit Entanglement Experiment



Conditions for generation and detection of qubit/photon entanglement

# Experimental Setup

- Transmon qubit

$$T_1 = 1.1 \mu s$$

$$T_2 = 550 ns$$

$$T_2^* = 220 ns$$

- Single sided resonator

$$1/\kappa = 25 ns$$

- Coupling strength

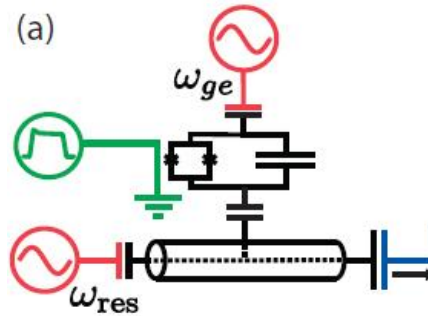
$$\pi/g = 7.7 ns$$

- Parametric amplifier

$$\sqrt{GB} = 178 \text{ MHz}$$

$$P_{1dB} @ \sim 16 \text{ photons}$$

Castellanos-Beltran *et al.*,  
*Nat. Phys.* 4, 929 (2008)



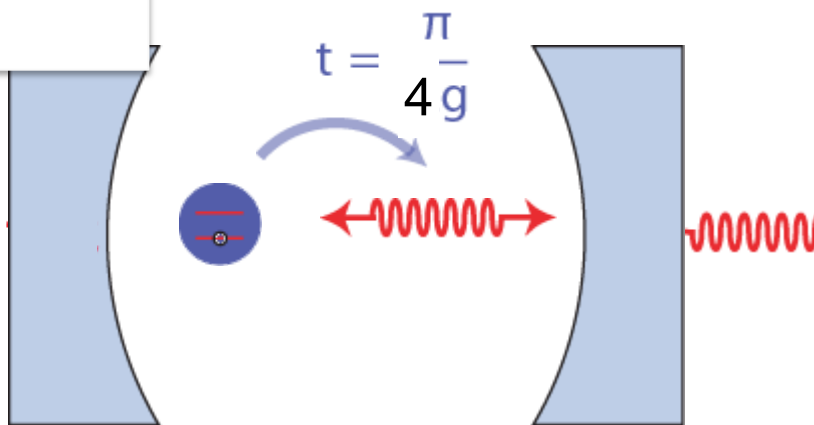
Detector = Paramp + ...

# Prepare and Measure Qubit/Photon Entanglement

## Step 2:

Entangle qubit with resonator by 1/4 vacuum Rabi oscillation

$$\frac{1}{\sqrt{2}} (|0e\rangle + |1g\rangle)$$

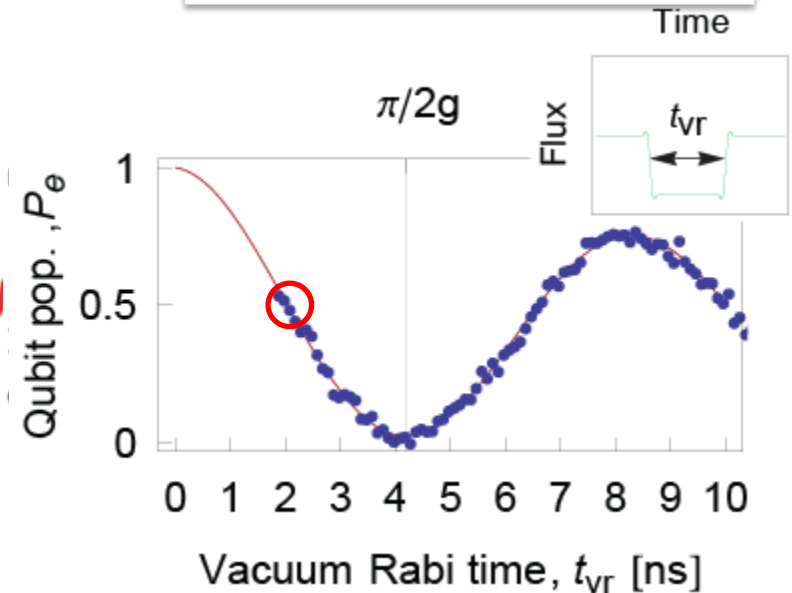


$$\alpha |g\rangle + \beta |e\rangle$$

$$\{ \text{qubit icons} \}$$

## Step 3:

Measure qubit and photon state.

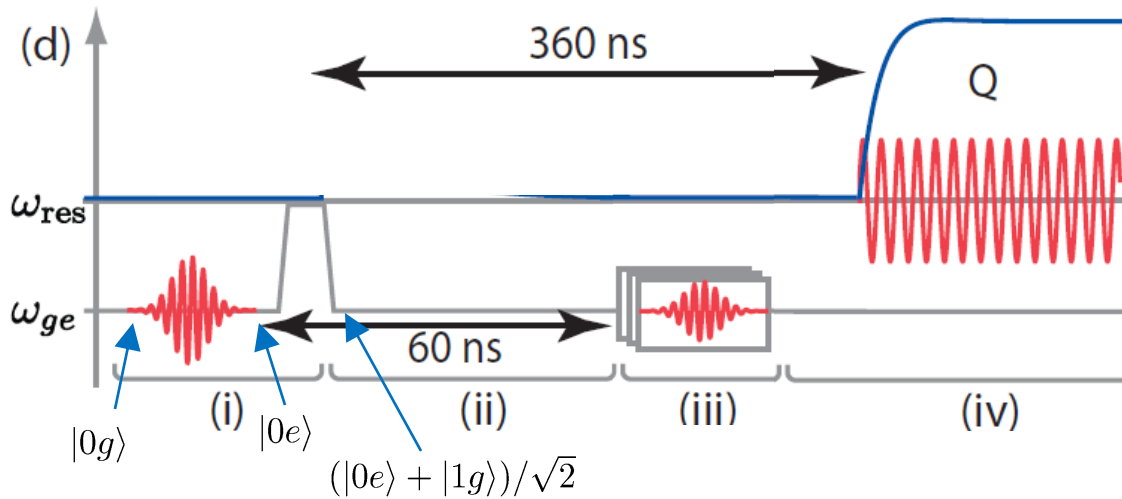


## Step 1:

Prepare qubit state by Rabi oscillation



# Exp. Entanglement Generation and Detection Sequence



(i) preparation of Bell state

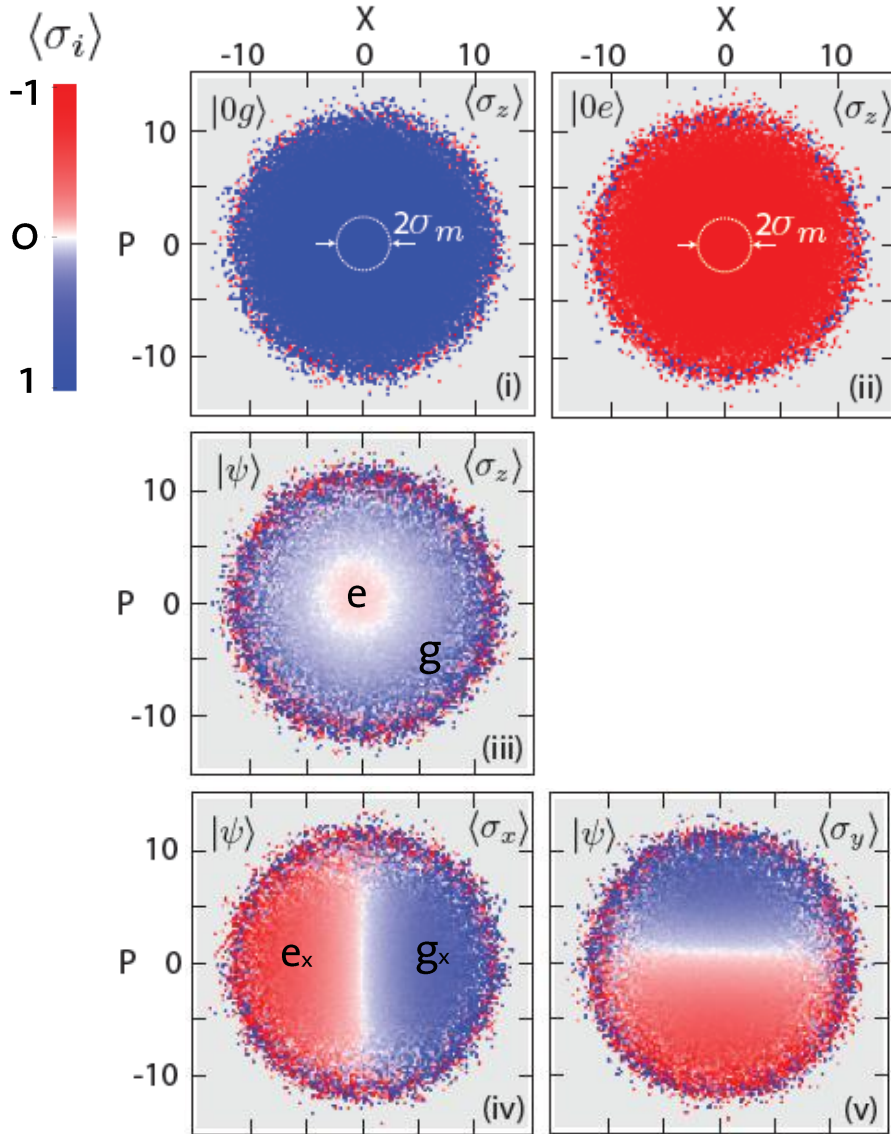
$$\frac{1}{\sqrt{2}} (|0e\rangle + |1g\rangle)$$

(ii) field decay into transmission line  
and measurement of X and P

(iii) qubit tomography pulses

(iv) dispersive qubit read-out

# Measurement Results



und state  
e  
ation vs.  
 $+ iP$



as expected  $\langle \sigma_z \rangle_\alpha$   
independent  
of  $\alpha$

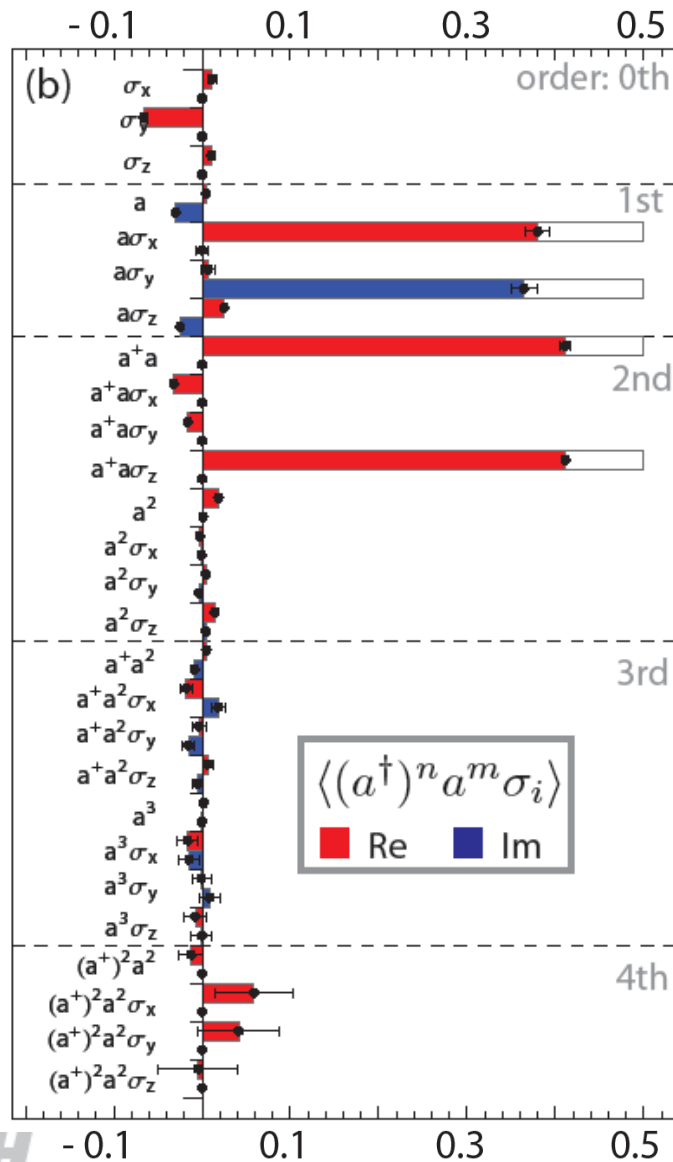
Analyzing the Bell state

$$|\psi\rangle = |0e\rangle + |1g\rangle$$

Probing coherences:

$$= |e_x\rangle \underbrace{(|1\rangle - |0\rangle)}_{\langle \hat{X} \rangle < 0} + |g_x\rangle \underbrace{(|1\rangle + |0\rangle)}_{\langle \hat{X} \rangle > 0}$$

# Extract Expectation Values of Moments of Distribution



0<sup>th</sup> : qubit state with photon traced out

1<sup>st</sup> : phase correlations between qubit and photon field

2<sup>nd</sup> : number correlations!

e <-> no photon

g <-> one photon

3<sup>rd</sup>, 4<sup>th</sup> : no higher photon number states!

exp: C. Eichler *et al.*, *arXiv:1209.0441* (2012)

theo: C. Eichler *et al.*, *Phys. Rev. A* **86**, 032106 (2012)

# Photon/Qubit Joint State Density Matrix

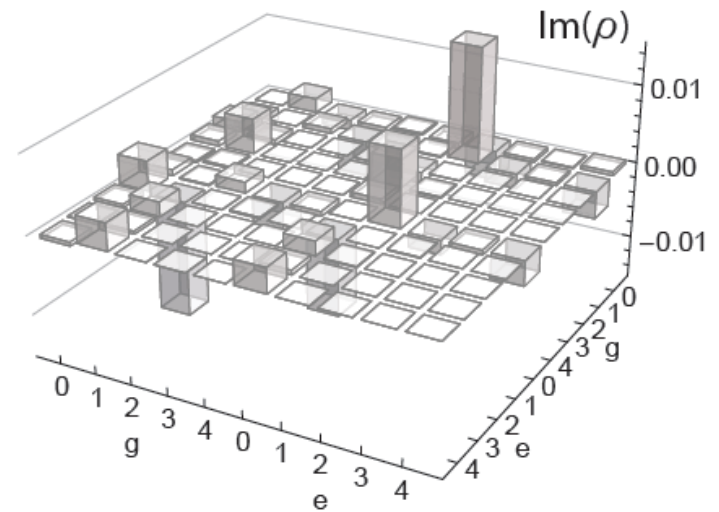
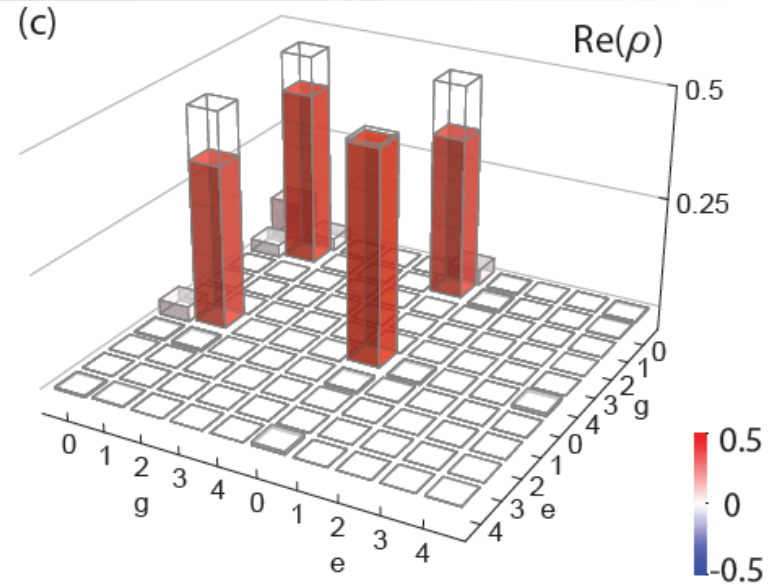
Reconstruction from measured moments

$$\text{Fidelity: } \langle \psi | \rho | \psi \rangle = 0.83$$

Limited by qubit decay during time required for photon detection in same mode.

Extension to states with more than a single photon possible, e.g.:

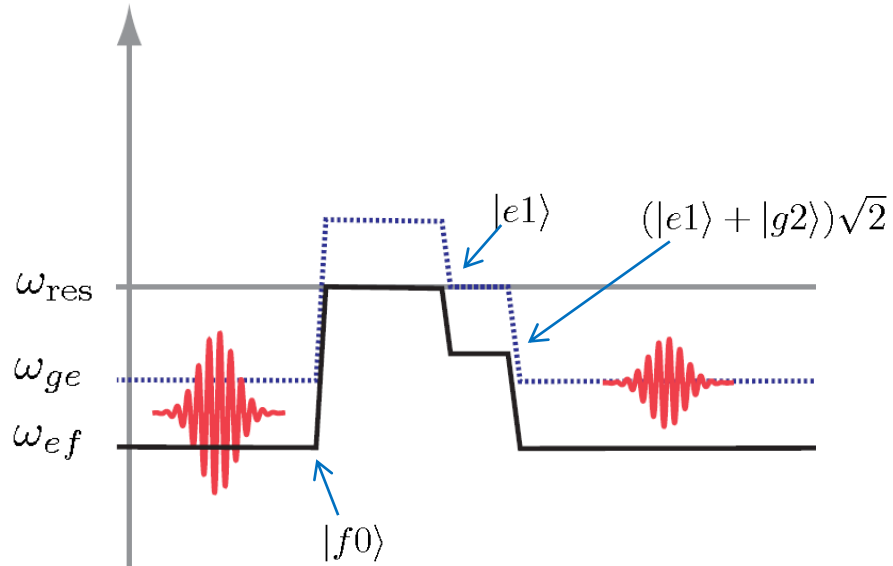
$$\frac{1}{2} [ |g\rangle(|1\rangle + |2\rangle) + |e\rangle(|1\rangle - |2\rangle) ]$$



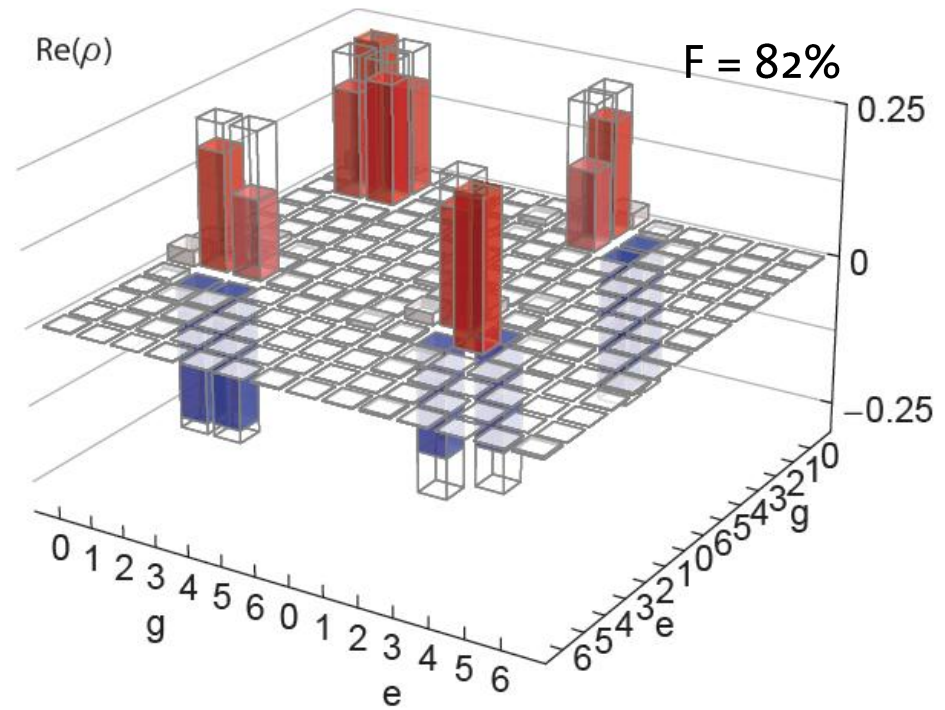
exp: C. Eichler *et al.*, *arXiv:1209.0441* (2012)  
theo: C. Eichler *et al.*, *Phys. Rev. A* **86**, 032106 (2012)

# Qubit Entangled with Two Propagating Photons

state:  $\frac{1}{2} [|g\rangle(|1\rangle + |2\rangle) + |e\rangle(|1\rangle - |2\rangle)]$   $\longrightarrow$  use second excited state of qubit for preparation



joint state tomography

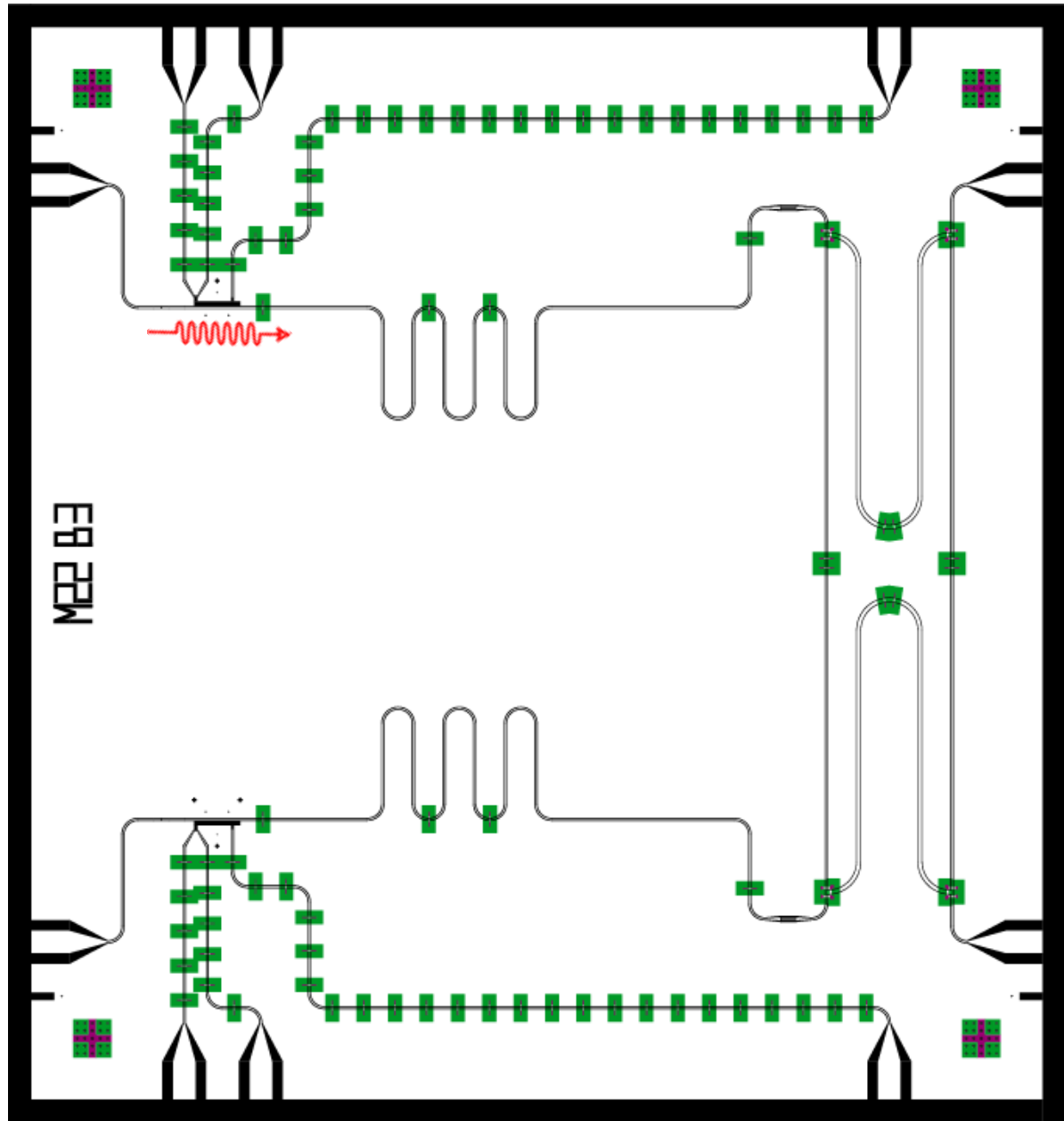


exp: C. Eichler *et al.*, *arXiv:1209.0441* (2012)  
 theo: C. Eichler *et al.*, *Phys. Rev. A* **86**, 032106 (2012)

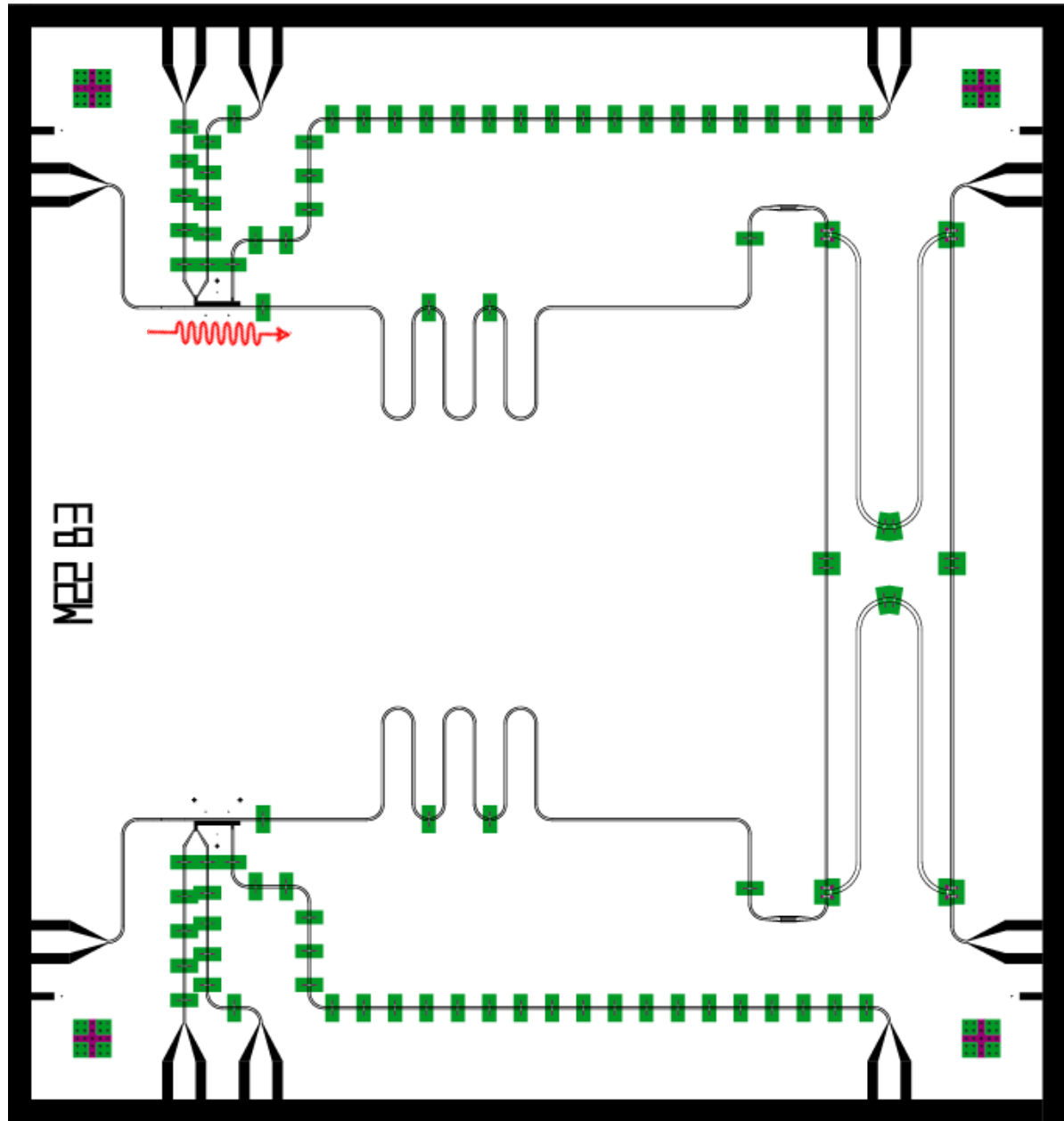
---

# **Two-Photon Interference: The Hong-Ou-Mandel Experiment with Microwaves**

# Design: Two Single Photon Sources and Beam Splitter

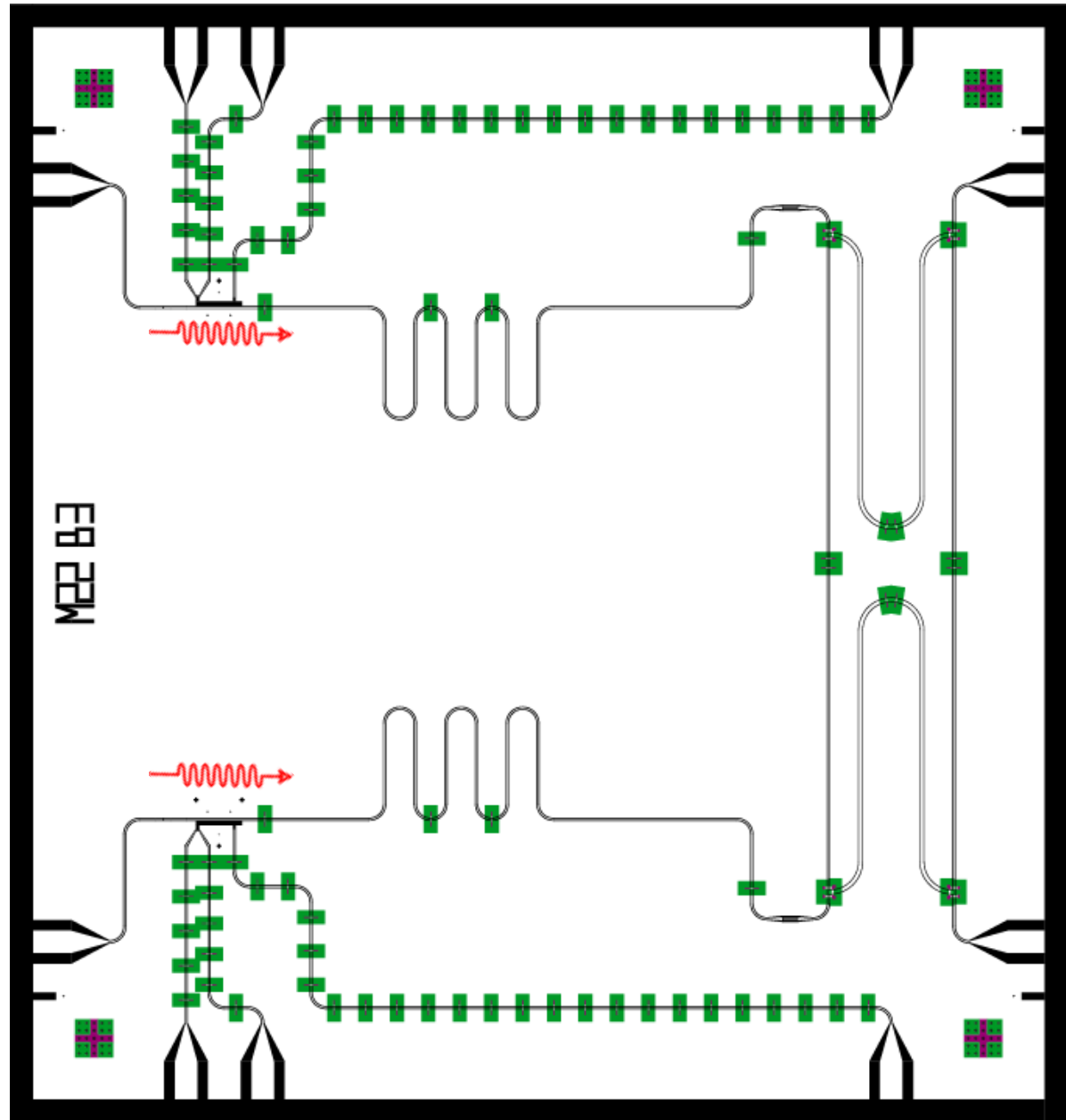


# Design: Two Single Photon Sources and Beam Splitter

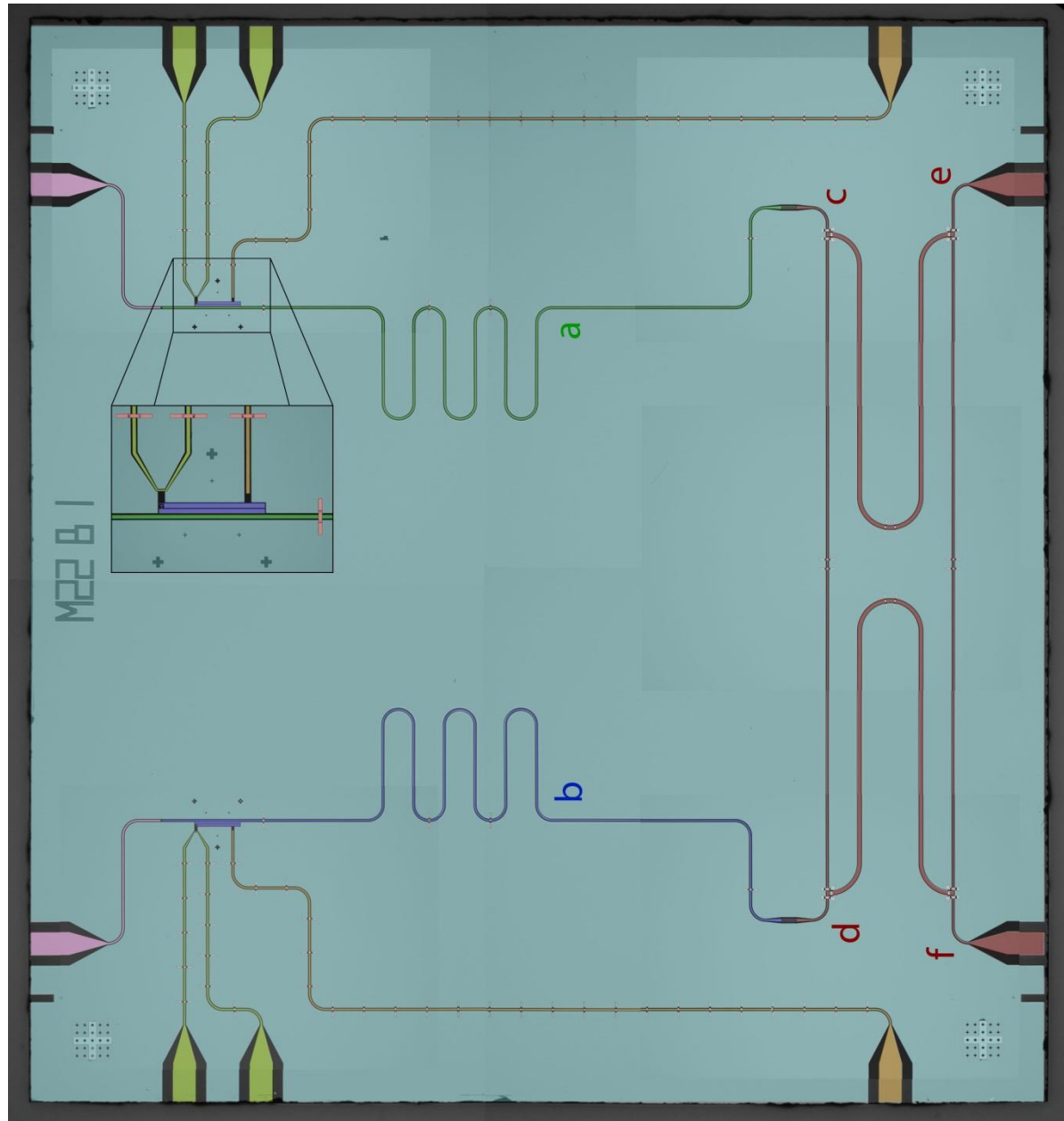




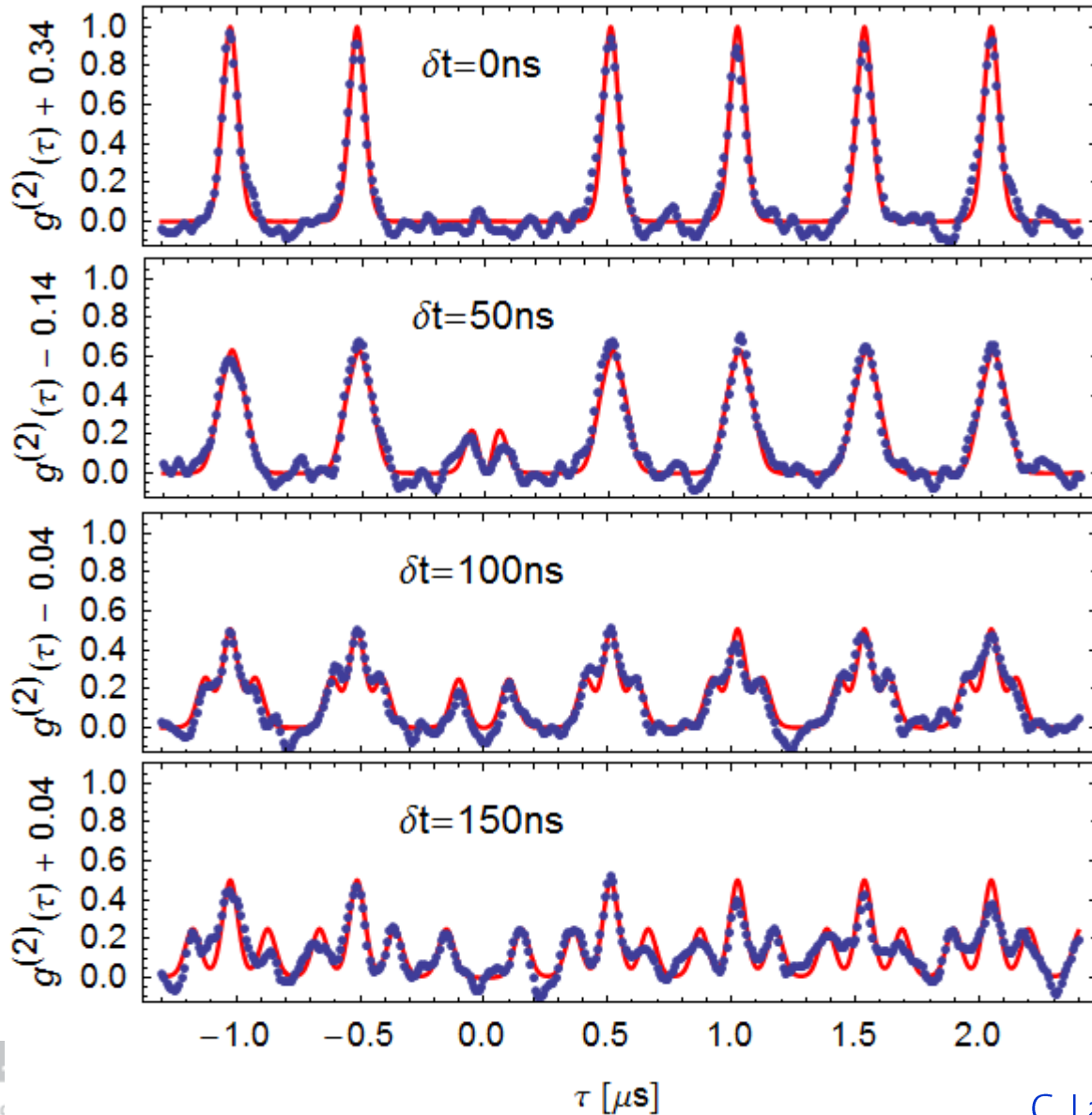
# Design: Two Single Photon Sources and Beam Splitter



# Design: Two Single Photon Sources and Beam Splitter



# Hong-Ou-Mandel $g^{(2)}(\tau)$ for Microwave Photons



Observations:

- Photon-Pair anti-bunching

For  $\tau > 0$ :

- Broadening of satellite peaks
- Triple-peak structure of satellite peaks
- Full recovery of double-peak at  $\tau \approx 0$

# Learning More: Two-Channel Tomography

Idea: Measure 4D histogram and evaluate relevant photon statistics

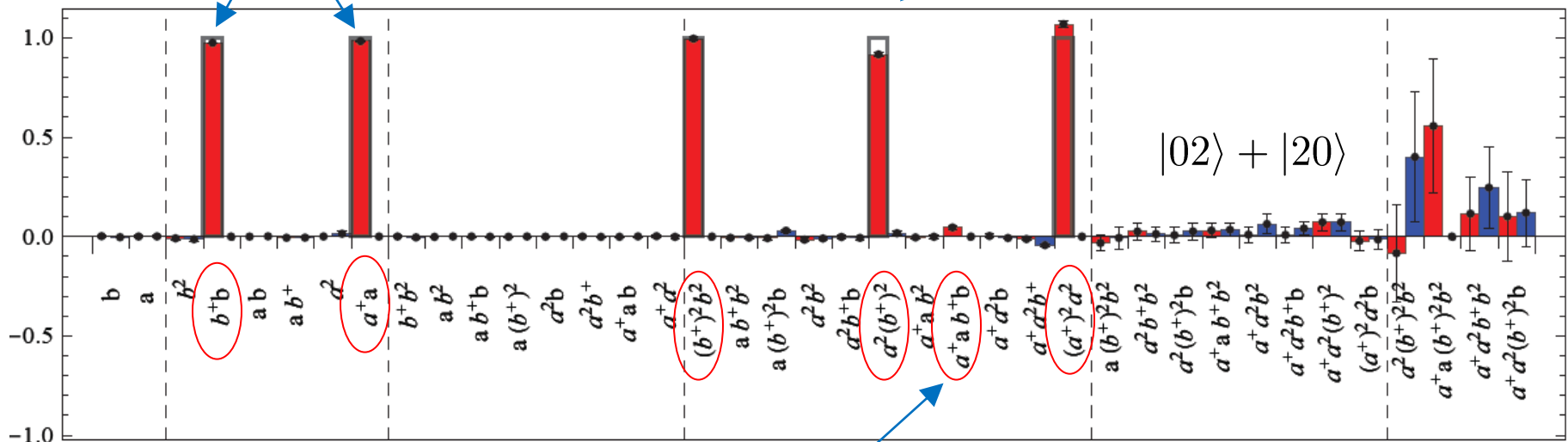
$$D_{\text{ON}}(X_a, P_a, X_b, P_b) \quad \xrightarrow{\text{analogous to}} \quad \langle (a^\dagger)^n a^m (b^\dagger)^k b^l \rangle$$

$$D_{\text{OFF}}(X_a, P_a, X_b, P_b) \quad \xrightarrow{\text{1-channel case}}$$

1 average photon  
in each channel

2-photon  
bunching

Quantum  
superposition!



never simultaneous  
“click” in both channels

# Density Matrix Displaying Two-Mode Entanglement

Density matrix reconstruction:

$$\langle (a^\dagger)^n a^m (b^\dagger)^k b^l \rangle$$

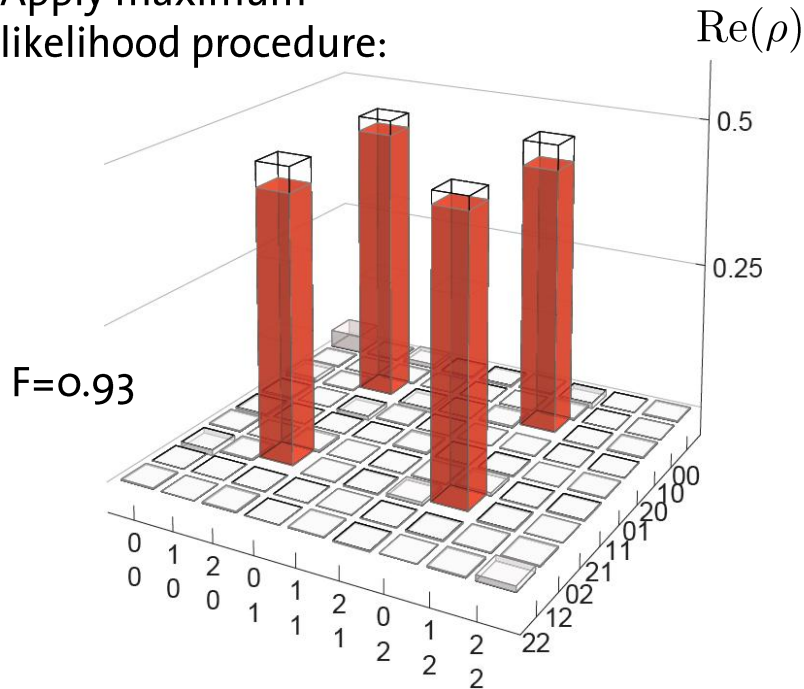
moments

linear map  
→

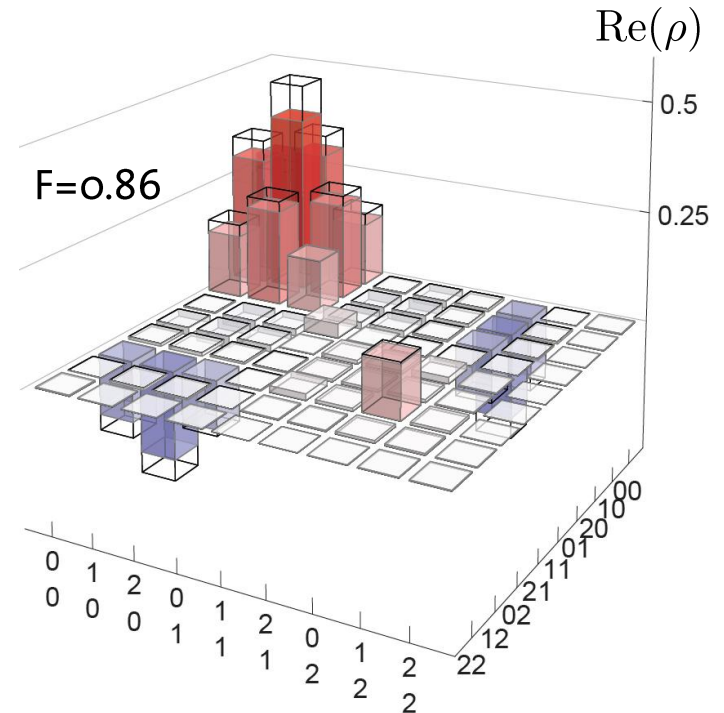
$$\langle nm | \rho | kl \rangle$$

Fock space  
density matrix

Apply maximum  
likelihood procedure:



$$|02\rangle + |20\rangle$$

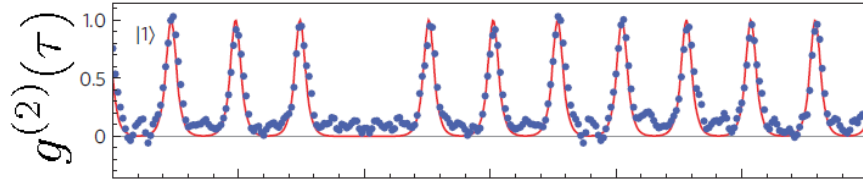


$$|00\rangle + \sqrt{2}|10\rangle + (|20\rangle - |02\rangle)\sqrt{2}$$

C. Lang, C Eichler *et al.*, ETH Zurich (2012)

# Experiments with Propagating Quantum Microwaves

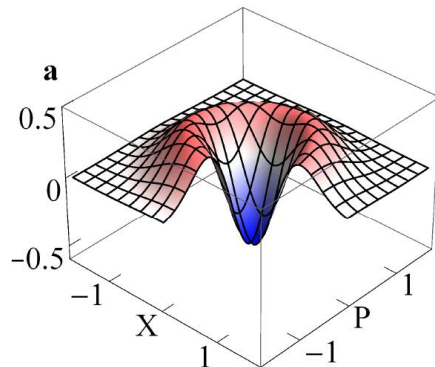
Single photon sources and their anti-bunching



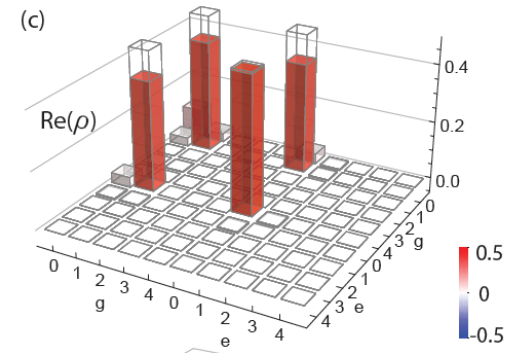
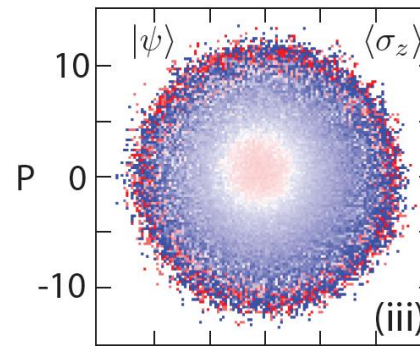
Bozyigit *et al.*, *Nat. Phys* 7, 154 (2011)  
Lang *et al.*, *PRL* 107, 073601 (2011)

Wigner functions and full state tomography of propagating photons:

Eichler *et al.*, *PRL* 106, 220503 (2011)



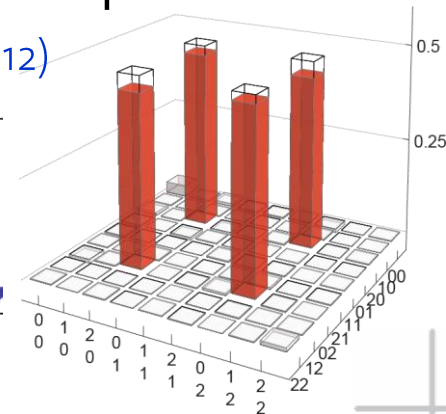
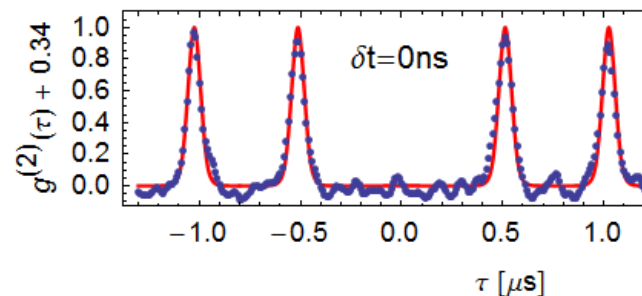
Preparation and characterization of qubit-propagating photon entanglement



Eichler *et al.*, *arXiv:1209.0441* (2012)  
Eichler *et al.*, *Phys. Rev. A* 86, 032106 (2012)

Hong-Ou-Mandel: Two-photon interference with coherences at microwave frequencies

Lang, Eichler *et al.*, *ETH Zurich* (2012)



# The ETH Zurich Quantum Device Lab

Postdoc and PhD positions available



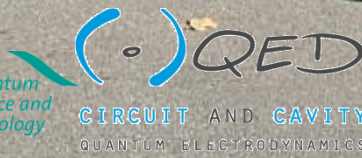
SWISS NATIONAL SCIENCE FOUNDATION



Eidgenössische Technische Hochschule Zürich  
Swiss Federal Institute of Technology Zurich



National Centre of Competence in Research



CIRCUIT AND CAVITY  
QUANTUM ELECTRODYNAMICS



# Selected Circuit QED Publications

## Circuit QED Proposal:

- Blais et al., *PRA* **69**, 062320 (2004)

## Strong Coupling & Vacuum Rabi Mode Splitting:

- Wallraff et al., *Nature* **431**, 162 (2004)
- Fink et al., *Nature* **454**, 315 (2008)
- Fink et al., *PRL* **105**, 163601 (2010)

## Tavis-Cummings Multi-Atom QED:

- Fink et al., *PRL* **103**, 083601 (2009)

## AC-Stark & Lamb Shift, Autler-Townes and Mollow Transitions

- Schuster et al., *PRL* **94**, 123062 (2005)
- Gambetta et al., *PRA* **74**, 042318 (2006)
- Schuster et al., *Nature* **445**, 515 (2007)
- Fragner et al., *Science* **322**, 1357 (2008)
- Baur et al., *PRL* **102**, 243602 (2009)

## Geometric Phases:

- Leek et al., *Science* **318**, 1889 (2007)
- Pechal et al., *PRL* **108**, 170401 (2012)

## One-, Two-, Three-Qubit Gates and Algorithms:

- Wallraff et al., *PRL* **95**, 060501 (2005)
- Blais et al., *PRA* **75**, 032329 (2007)
- Wallraff et al., *PRL* **99**, 050501 (2007)
- Majer et al., *Nature* **449**, 443 (2007)
- Leek et al., *PRB* **79**, 180511(R) (2009)
- Filipp et al., *PRL* **102**, 200402 (2009)
- Leek et al., *PRL* **104**, 100504 (2010)
- Bianchetti et al., *PRL* **105**, 223601 (2010)
- Fedorov et al., *Nature* **481**, 170 (2012)
- Baur et al., *PRL* **108**, 040502 (2012)
- Steffen et al., *PRL* **108**, 260506 (2012)

## Device Fabrication:

- Frunzio et al., *IEEE Trans. Appl. Sup.* **15**, 860 (2005)
- Goeppel et al., *J. Appl. Phys.* **104**, 113904 (2008)

## Review (gr.):

- Wallraff, *Physik Journal* **7** (12), 39 (Dez. 2008)

Additional Information: [www.qudev.ethz.ch](http://www.qudev.ethz.ch)



# Selected Circuit QED Publications (cont'd)

Itinerant Photons, Tomography, Photon Blockade,

Correlation Functions:

- da Silva et al., *PRA* **82**, 043804 (2010)
- Bozyigit et al., *Nat. Phys.* **7**, 154 (2011)
- Eichler et al., *PRL* **106**, 220503 (2011)
- Lang et al., *PRL* **106**, 243601 (2011)
- Eichler et al., *PRL* **107**, 113601 (2011)
- Eichler et al., *PRA* **86**, 032106 (2012)
- Eichler et al., arXiv:1209.0441 (2012)

Hybrid Systems:

- Frey et al., *PRL* **108**, 046807 (2012)
- Frey et al., *PRB* **86**, 115303 (2012)
- Hogan et al., *PRL* **108**, 063004 (2012)