

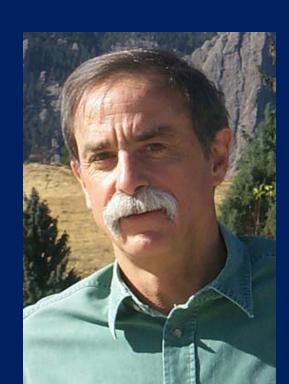
Quantum computation and simulation with cold ions

Jonathan Home

Dave Wineland and Serge Haroche

Nobel Prize in Physics 2012

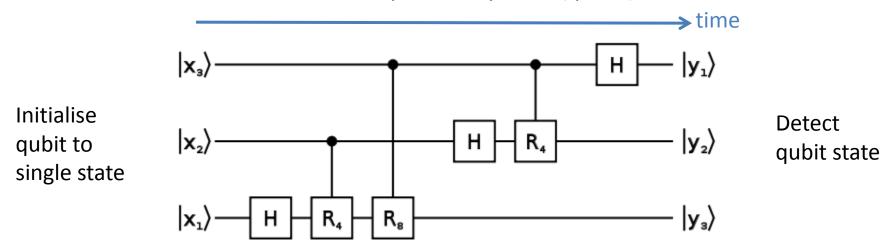
"for ground-breaking experimental methods that enable measuring and manipulation of individual quantum systems"



Quantum computation

(Precision control of large-scale quantum mechanical systems)

David Deutsch: Collection of two-state quantum systems (qubits)



Operations which manipulate isolated qubits or pairs of qubits

Large scale device:

Transport information around processor/distribute entangled states

Perform operations accurately enough to achieve fault-tolerant error-correction (reach arbitrary size system) – accuracy of 0.9999 required

Isolating single charged atoms

Laplace's equation

– no chance to trap with static fields

$$\frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} + \frac{\partial^2 V}{\partial z^2} = 0$$

Paul trap: Use a ponderomotive potential – change potential fast compared to speed of ion

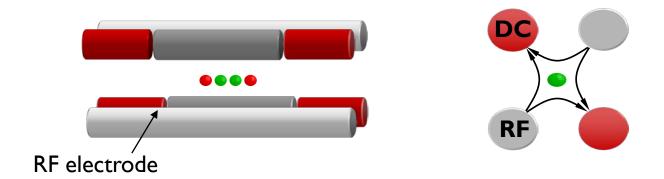
$$\frac{\partial^2 V}{\partial x^2} + \left(\frac{\partial^2 V}{\partial y^2} + \frac{\partial^2 V}{\partial z^2}\right) \cos(\Omega t)$$

$$M\frac{d^2x}{dt^2} = qE\cos\Omega t$$

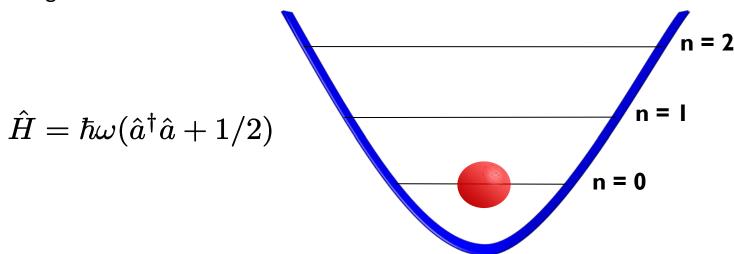
$$\frac{1}{2}M\left(\frac{dx}{dt}\right)^2 = U_{\rm PP} = \frac{q^2E^2}{2M\Omega^2}\sin^2\Omega t$$

Time average - Effective potential energy which is minimal at minimum E

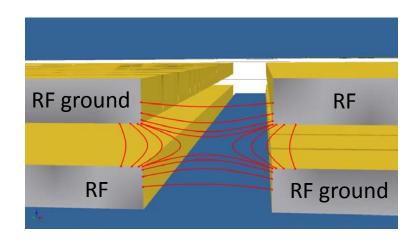
Traps – traditional style

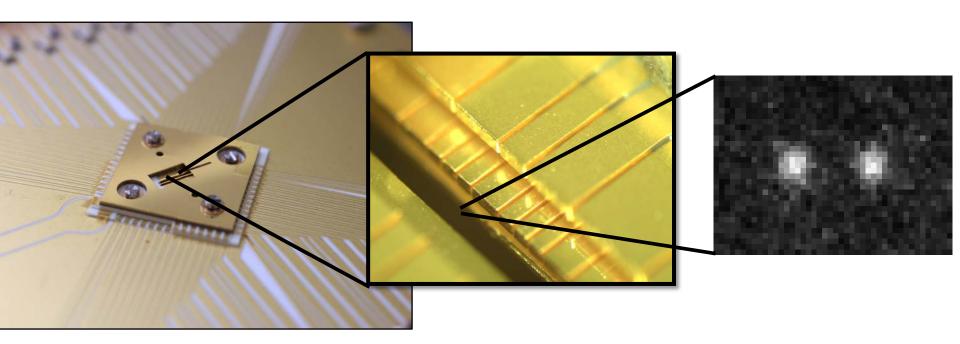


Axial potential gives almost ideal harmonic behaviour



Ion traps at ETH Zurich





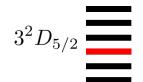
Storing a qubit in multi-level atoms

$$|\psi\rangle = (a|0\rangle + b|1\rangle)$$

⁴⁰Ca⁺ - fine structure

$$M_J = -3/2 \qquad -1/2 \qquad 4^2 P_{3/2}$$

$$4^2P_{1/2}$$
 $-1/2$ $1/2$



$$3^2D_{3/2}$$

$$4^2S_{1/2}$$
 1/2 $-1/2$

⁹Be⁺ - hyperfine structure

$$^2P_{3/2}$$
 (16 Hyperfine states)

$$^{2}P_{1/2}$$

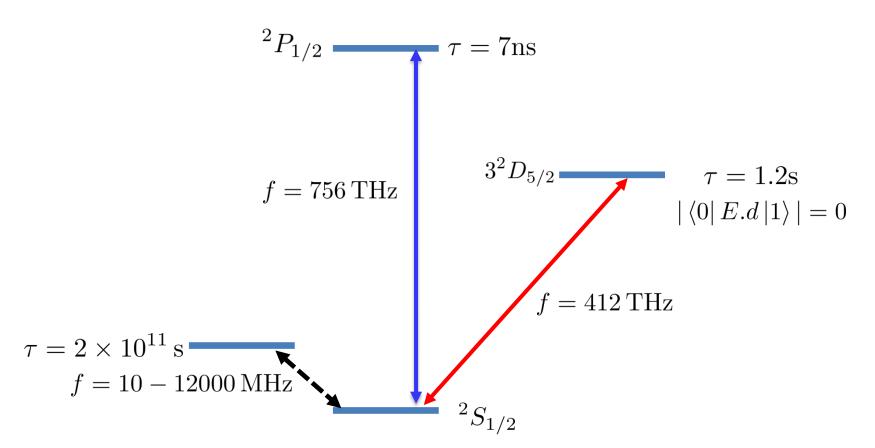
$$^2S_{1/2}$$

Choice of qubit levels

$$|\psi\rangle = (a|0\rangle + b|1\rangle)$$

Requirement: long decay time for upper level.

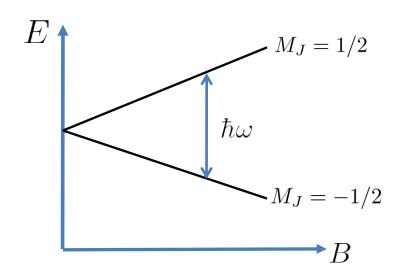
$$au \propto rac{1}{\omega^3} rac{1}{|\langle 0|E.d|1\rangle|^2}$$

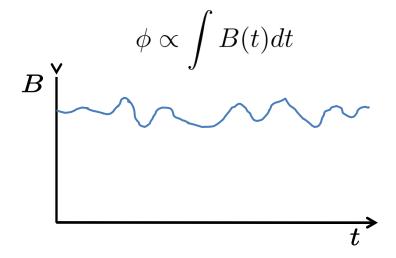


Storing qubits in an atom - phase coherence

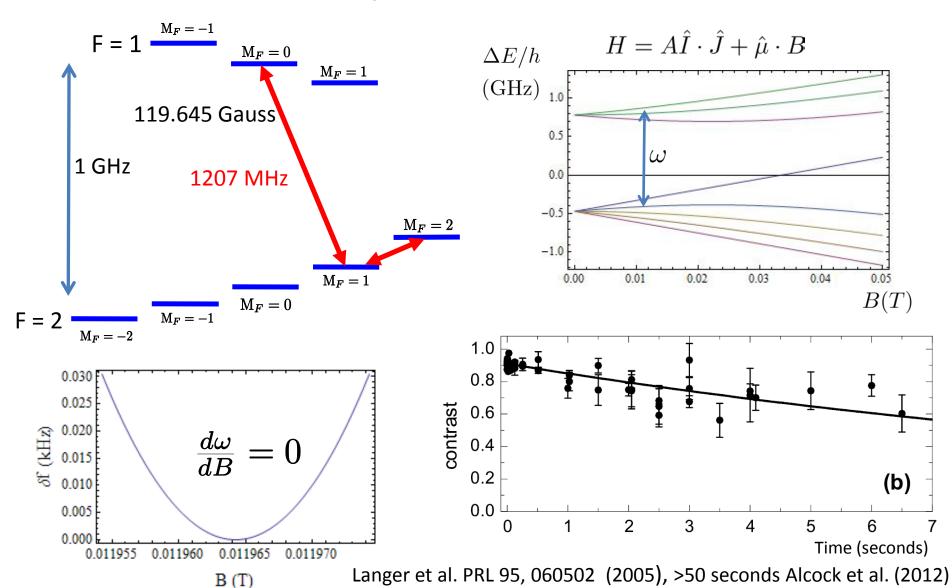
$$|\psi\rangle = (a|0\rangle + be^{i\phi}|1\rangle)$$

Problem: noise! – mainly from classical fields





Storing qubits in an atom Field-independent transitions



Entanglement for protection

Rejection of common-mode noise

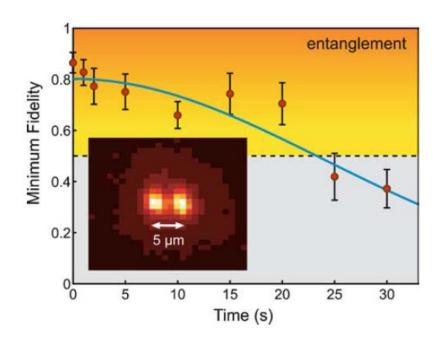
$$|0\rangle + e^{i\omega'(t)t}|1\rangle$$

$$|0\rangle + e^{i\omega(t)t} |1\rangle$$

Now consider entangled state

$$e^{i\omega(t)t} |01\rangle + e^{i\omega'(t)t} |10\rangle = e^{i\omega(t)t} \left(|01\rangle + e^{i(\omega'(t) - \omega(t))t} |10\rangle \right)$$

If noise is common mode, entangled states can have very long coherence times

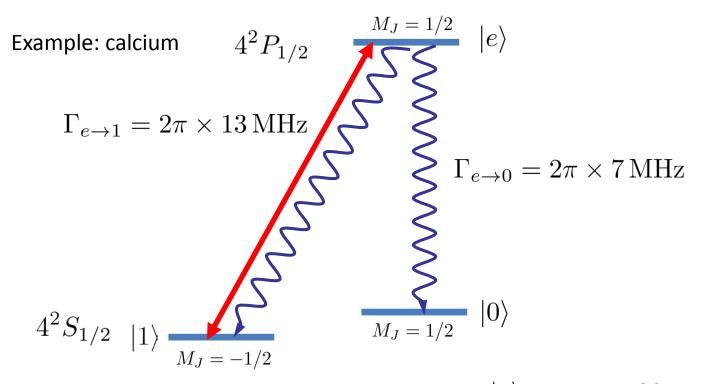


Haffner et al., Appl. Phys. B 81, 151-153 (2005)

Preparing the states of ions

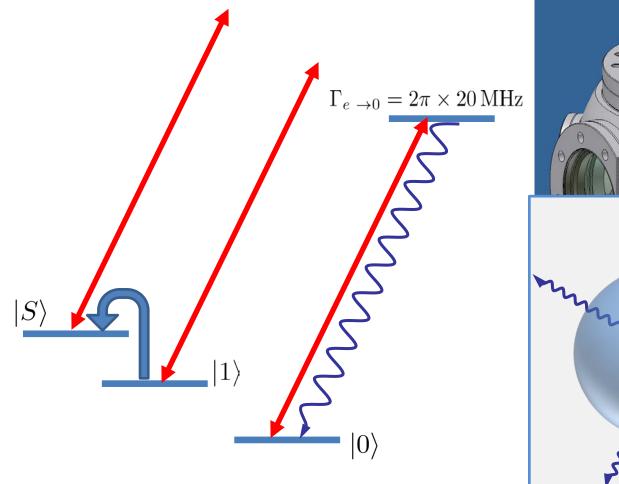
Optical pumping – state initialisation

Use a dipole transition for speed



Calcium: scatter around 3 photons to prepare |0
angle $au_{
m prep} \sim 20\,{
m ns}$

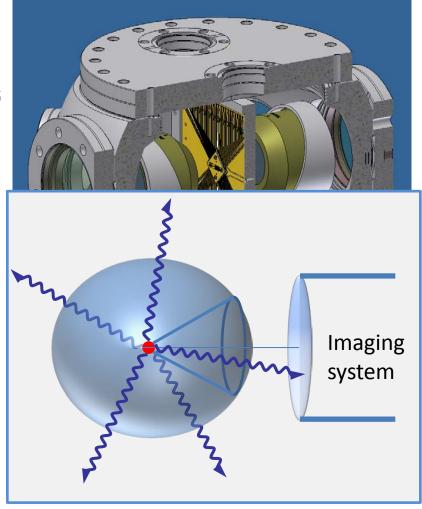
Reading out the quantum state



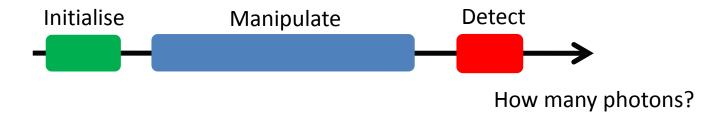
Photon scattered every 7 ns **BUT**

we only collect a small fraction of these

Need to scatter 1000 photons to detect atom $T_{
m readout} \sim 100
ightarrow 1000 \, \mu {
m s}$

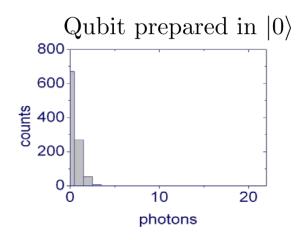


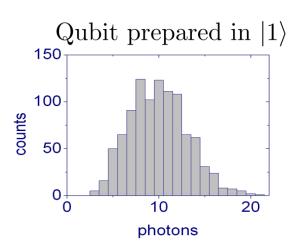
Measurement – experiment sequence



Statistics: repeat the experiment many (1000) times

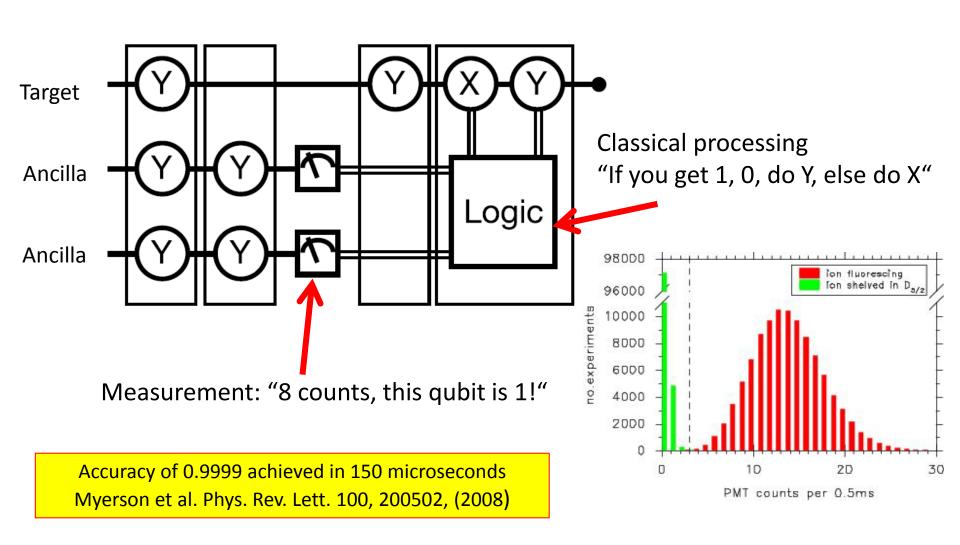
Number of photons = 8, 4, 2, 0, 0, 1, 5, 0, 0, 8





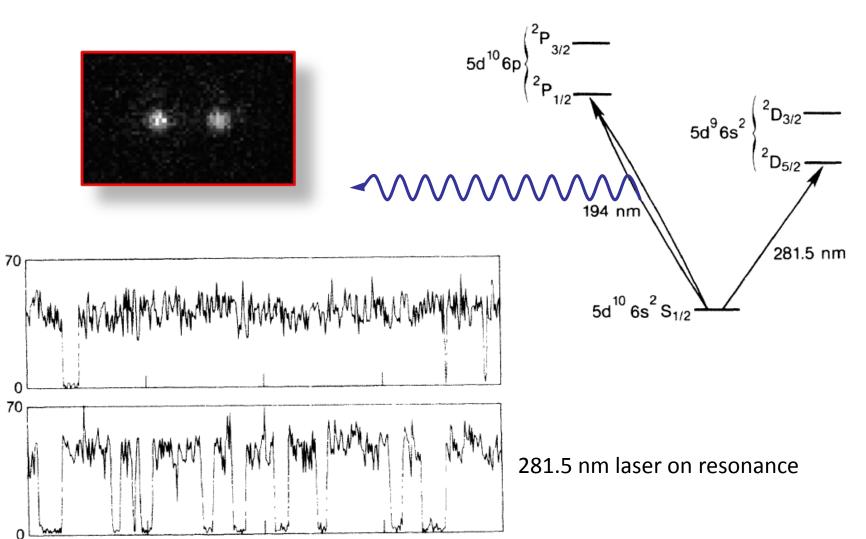
Single shot measurement

"Realization of quantum error-correction", Chiaverini et al., Nature 432, 602, (2004)



Quantum jumps of a single atom

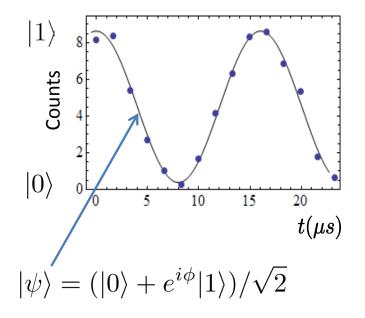
Bergquist et al. PRL 57, 14, (1986)

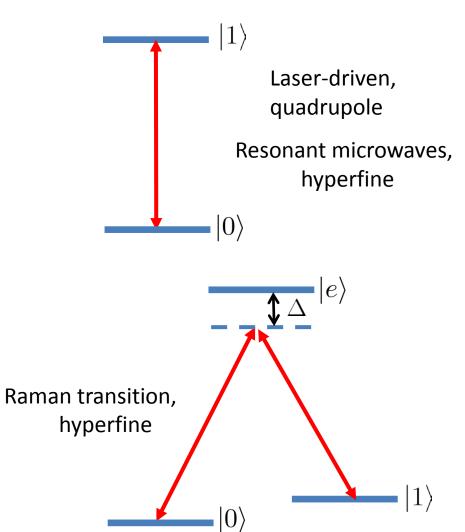


time

Manipulating single qubits

$$H = \Omega(|0\rangle\langle 1| + |1\rangle\langle 0|)\cos(\omega t + \phi)$$



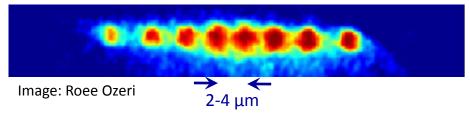


Lowest error rate $\sim 1 \times 10^{-6}$

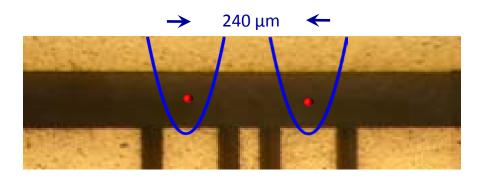
Addressing individual qubits

Intensity addressing

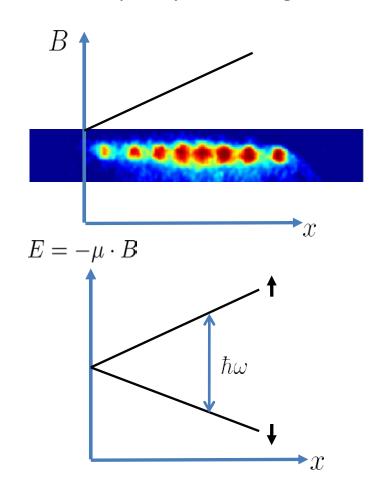
Shine laser beam at one ion in string



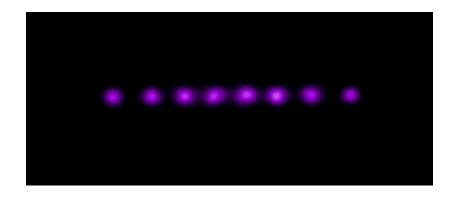
Separate ions by a distance much larger than laser beam size



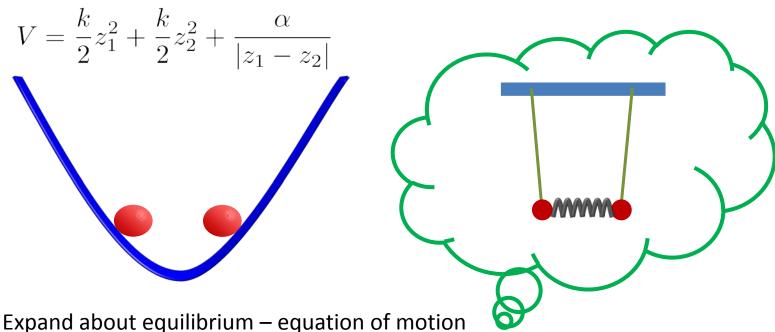
Frequency addressing



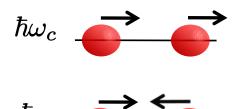
Multiple qubits: interactions



Multiple ions: coupled harmonic oscillators



$$\begin{pmatrix} \ddot{\epsilon}_1 \\ \ddot{\epsilon}_2 \end{pmatrix} = -\omega_z^2 \begin{pmatrix} \epsilon_1 \\ \epsilon_2 \end{pmatrix} = \begin{pmatrix} k & \alpha \\ \alpha & k \end{pmatrix} \begin{pmatrix} \epsilon_1 \\ \epsilon_2 \end{pmatrix}$$

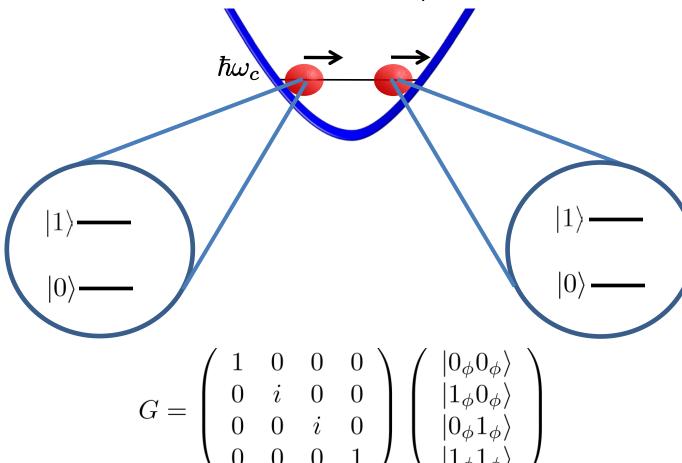


Independent oscillators - shared motion

The original thought

Cirac and Zoller, PRL (1995)

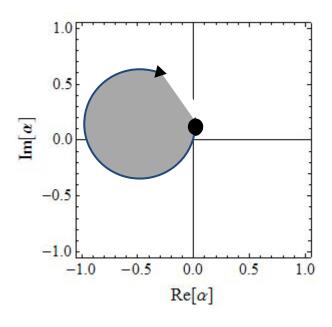
"The collective oscillator is a quantum bus"



The forced harmonic oscillator

Classical forced oscillator

$$\frac{d^2x}{dt^2} = -\omega_z^2 x + \frac{F}{m}\cos(\omega t + \phi)$$



"returns" after
$$t=\frac{2\pi}{\delta}$$
 Radius of loop $\propto \frac{F}{\delta}$

Forced quantum oscillators

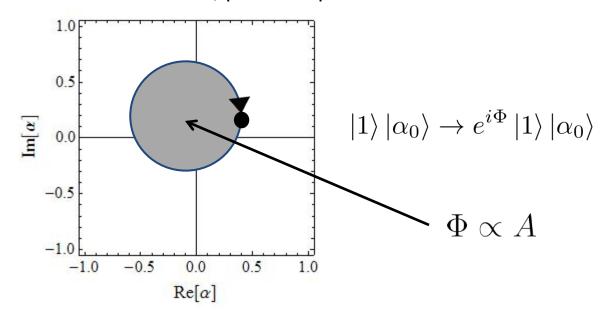
$$H(t) = \Omega \cos(\omega t) e^{ikz}$$

$$\simeq \Omega \cos(\omega t) \left(1 + ikz_0 \left(\hat{a}e^{i\omega_z t} + \hat{a}^{\dagger}e^{-i\omega_z t}\right)\right)$$

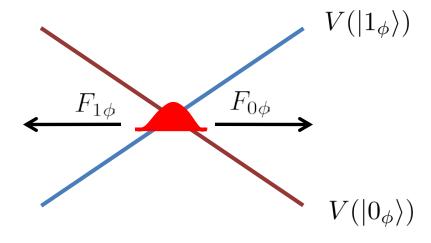
$$\left[H(t), H(t')\right] \neq 0$$

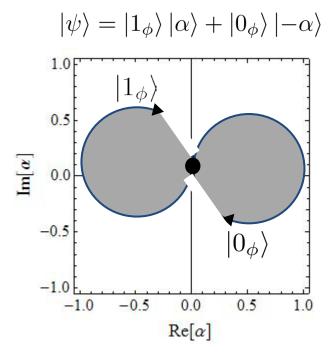
$$U = \exp\left(\frac{i}{\hbar} \int^t H(t')dt' - \frac{1}{2\hbar^2} \int^t \int^{t'} [H(t'), H(t'')]dt'dt'' + \dots\right)$$

Transient excitation, phase acquired



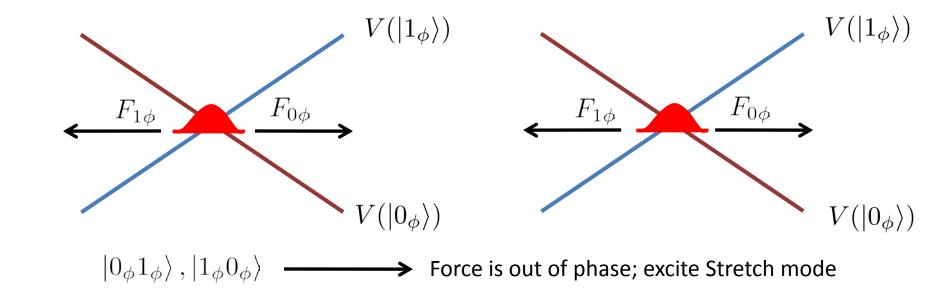
State-dependent excitation

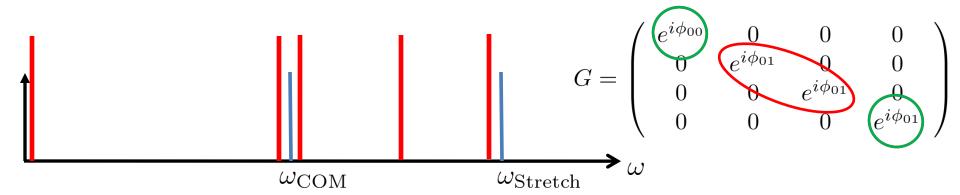




Entangled spin-motion state "Schrodinger's cat"

Two-qubit gate, state-dependent excitation



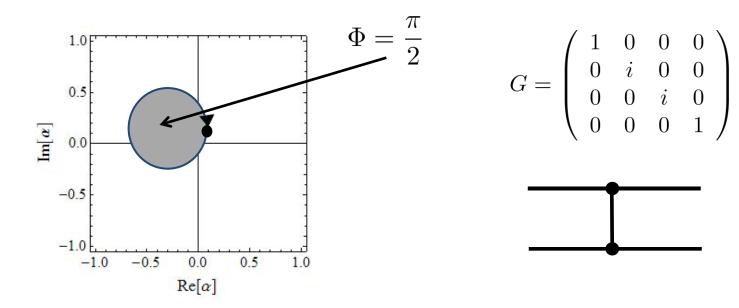


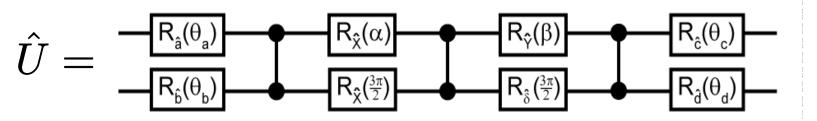
Force is in-phase; excite COM mode

 $|1_{\phi}1_{\phi}\rangle, |0_{\phi}0_{\phi}\rangle$

Examples: quantum computing

Choose the duration and power: $t_g = 2\pi/\delta \sim 7 \rightarrow 100 \mu s$

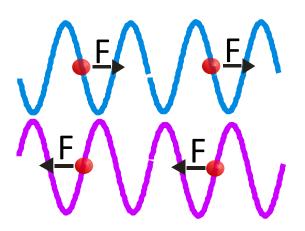




Universal two-qubit ion trap quantum processor: Hanneke et al. Nature Physics 6, 13-16 (2010)

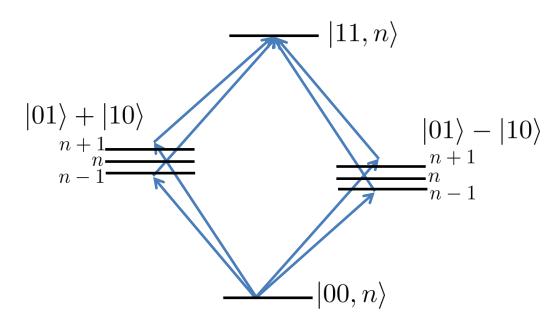
Laser-driven multi-qubit gates

 σ_z basis, polarisation standing wave Leibfried et al. Nature 422, 412-415 (2003)

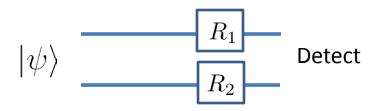


$$G = \left(\begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & i & 0 & 0 \\ 0 & 0 & i & 0 \\ 0 & 0 & 0 & 1 \end{array}\right)$$

 σ_x, σ_y basis, interference effect

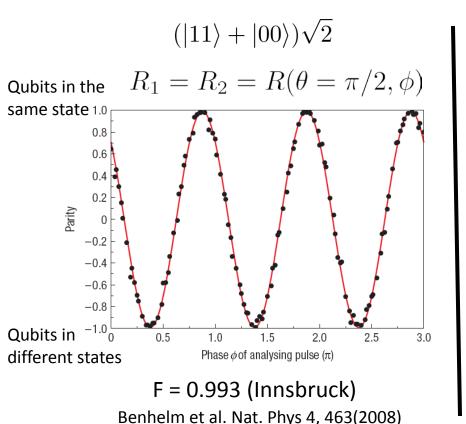


State and entanglement characterisation



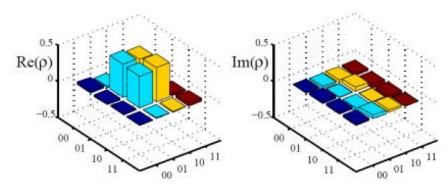
8, 6, 7, 4, 9, 0, 0, 1, 1, 6, 1, 9, 0, 0... 5, 4, 3,11, 4, 1, 0, 0, 1, 8, 0, 8, 1, 0...

Entanglement – correlations...



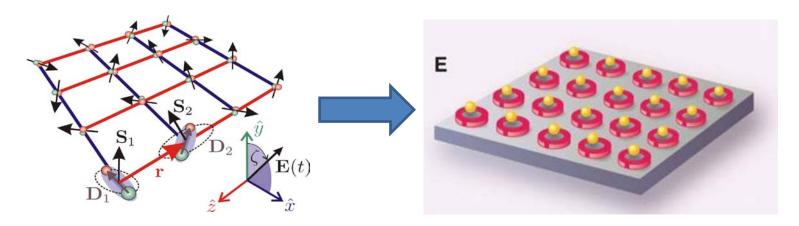
Choose 12 different settings of R_1, R_2

Reconstruct density matrix



Quantum simulation with trapped-ions

Creation of "condensed-matter" Hamiltonians with long-range interactions (Friedenauer et al. Nat. Phys 4, 757-761 (2008), Kim et al. Nature 465, 7298 (2010))



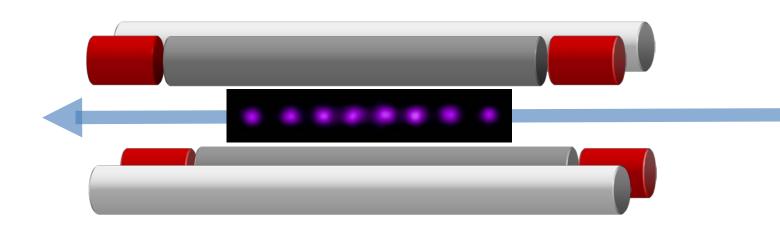
Go to limit of large motional detuning (very little entanglement between spin and motion)

$$\Omega \ll \delta$$

$$\Phi_{10} = \Phi_{01} \simeq i \frac{\Omega^2}{\delta} t$$

$$H_{\mathrm{eff}} \simeq rac{\Omega^2}{\delta} s_1^x s_2^x \qquad H_{\mathrm{eff}} \simeq rac{\Omega^2}{\delta} \sum_{i
eq i}^N s_i^x s_j^x$$

Dealing with large numbers of ions



Technical	requirement
iccillical	requirement

Spectral mode addressing

Many ions

Simultaneous laser addressing

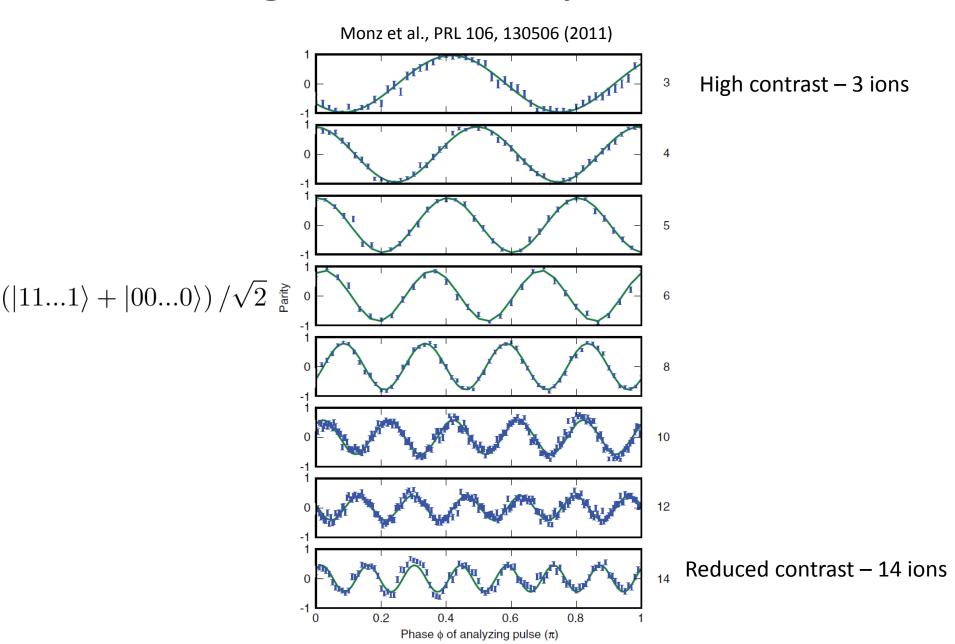
Limitation

Mode density increases

Heating rates proportional to N

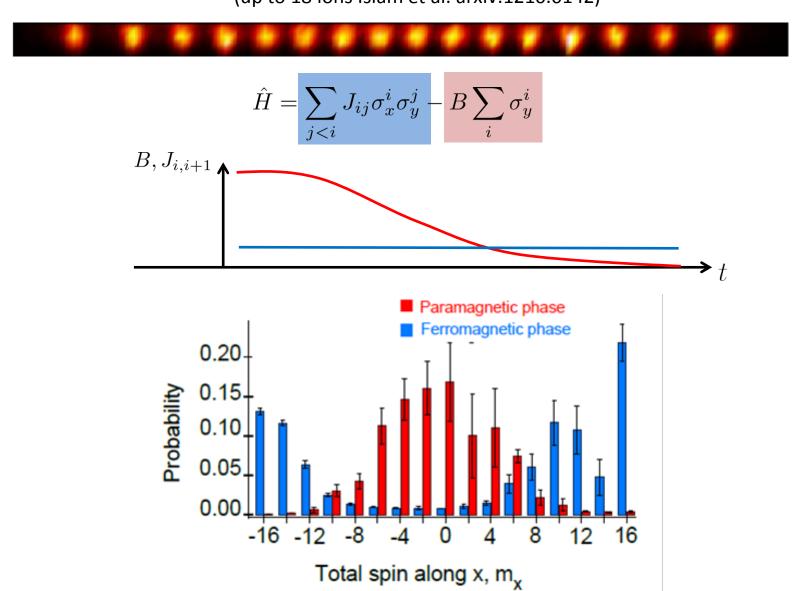
Ions take up space (separation > 2 micron)
Laser beams are finite-size

Entanglement of up to 14 ions



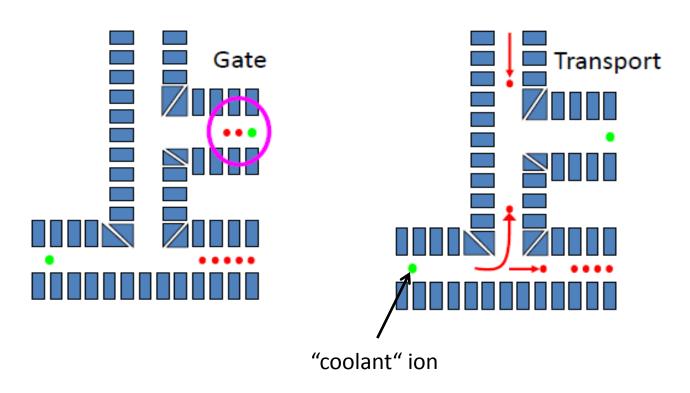
Quantum simulations in ion strings

(up to 18 ions Islam et al. arxiv:1210.0142)



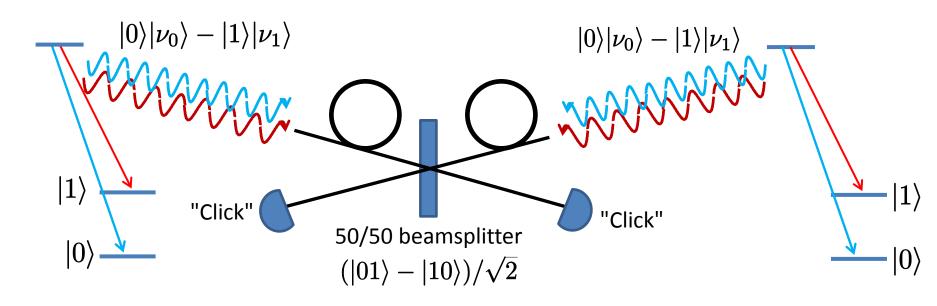
Isolate small numbers of ions

Wineland et al. J. Res. Nat. Inst. St. Tech, (1998)

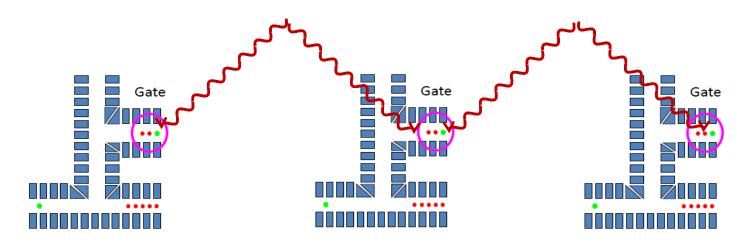


Technological challenge – large numbers of electrodes, many control regions

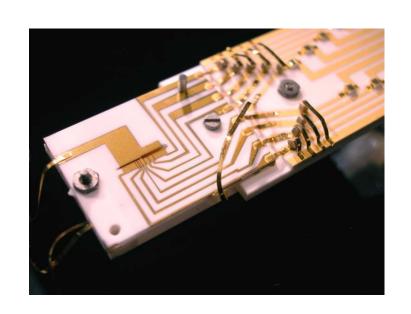
Distributing entanglement: probabilistic

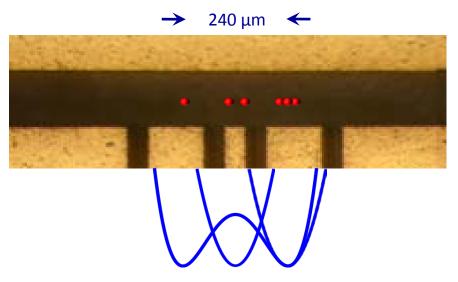


Entangled ions separated by 1m (Moehring et al. Nature 449, 68 (2008))



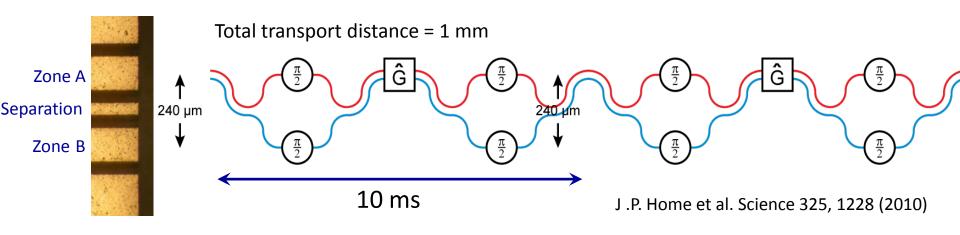
Transport with ions





Move: 20 us, Separate 340 us, 0.5 quanta/separation

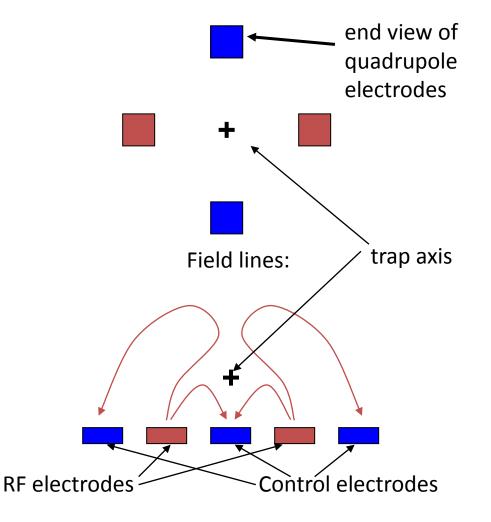
Internal quantum states of ions unaffected by transport **Motional** states are affected – can be re-initialised

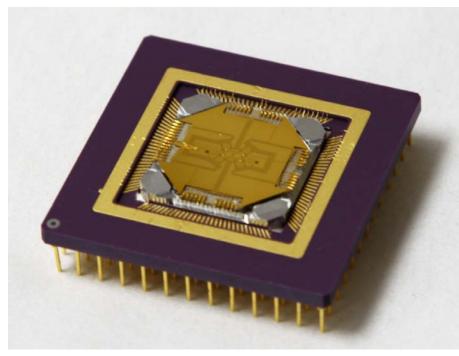


Trapping ions on a chip

For microfabrication purposes, desirable to deposit trap structures on a surface

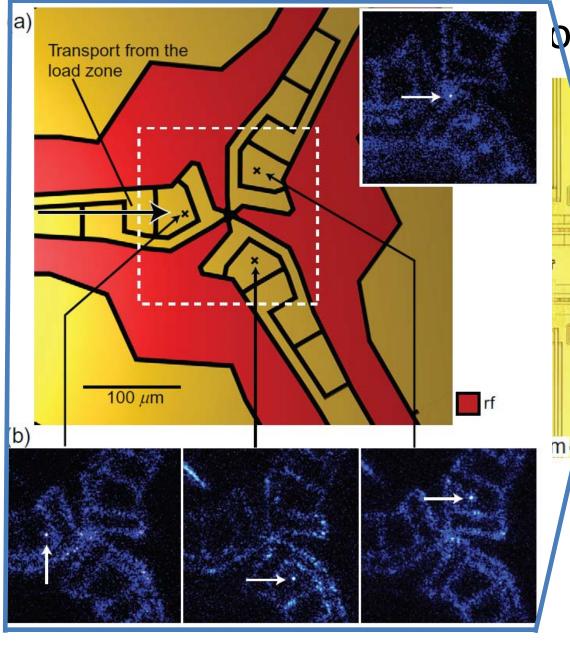
(Chiaverini et al., Quant. Inf. & Computation (2005), Seidelin et al. PRL 96, 253003 (2006))



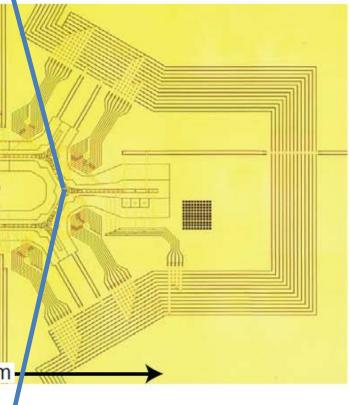


Challenges: shallow trap depth (100 meV) charging of electrodes

Opportunities: high gradients

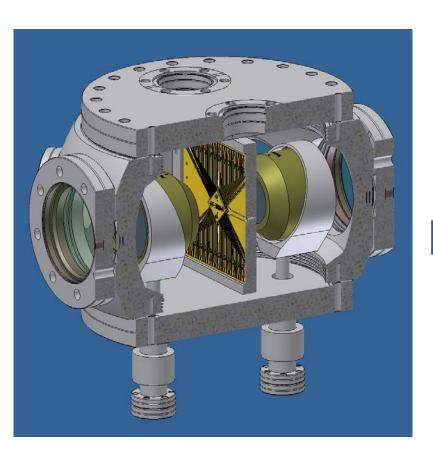


emplicated) chip

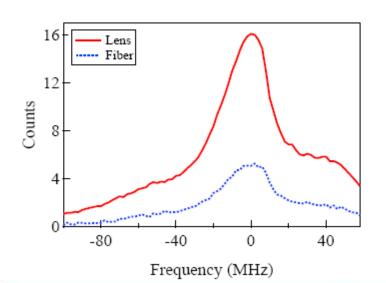


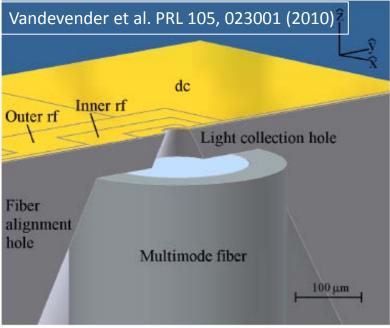
J. Amini et al. New. J. Phys 12, 033031 (2010)

Integrated components 1



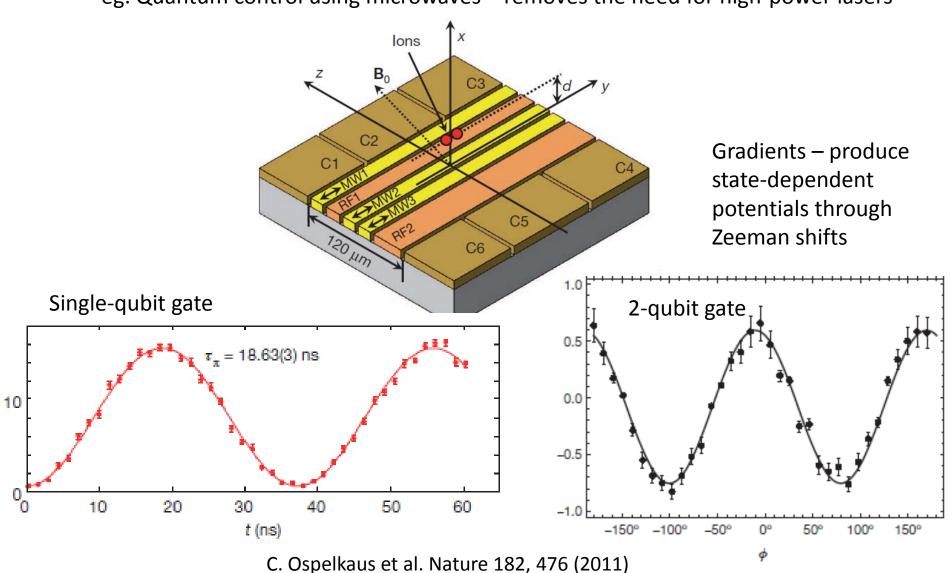






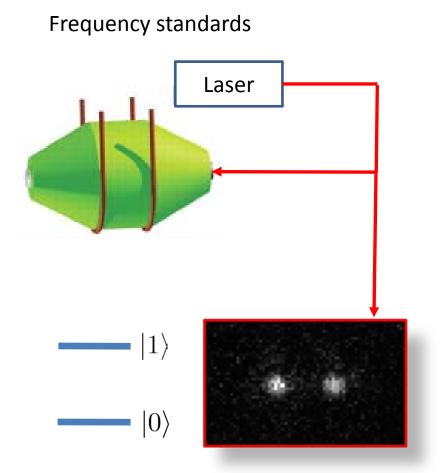
Integrated components

eg. Quantum control using microwaves – removes the need for high-power lasers

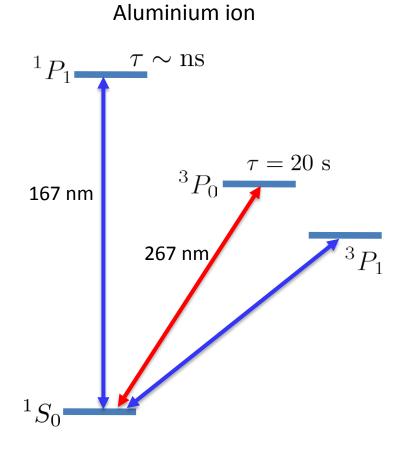


Trapped-ions and optical clocks

e.g. Rosenband et al., Science 319, 1808 (2008)

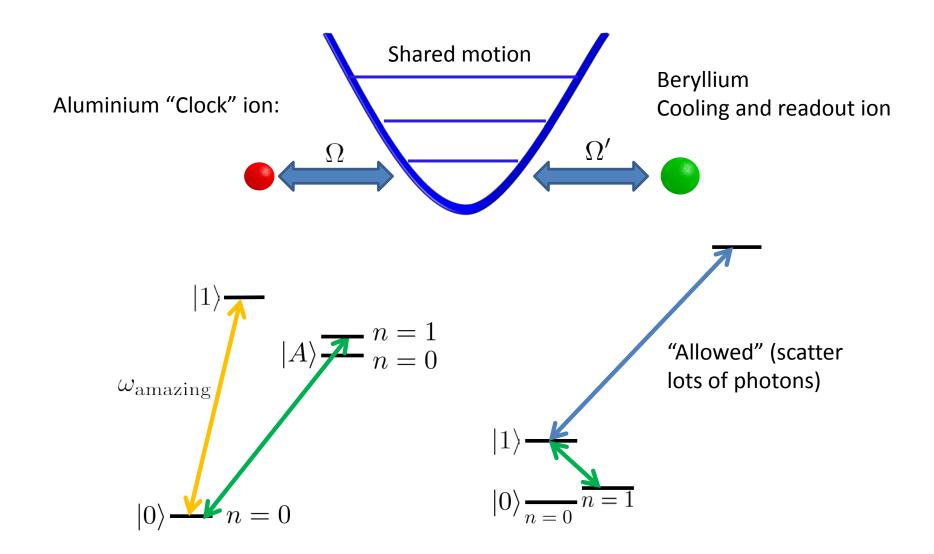


Require very stable ion transition



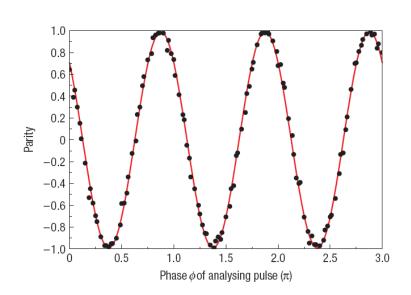
Has a very stable transition BUT 167 nm is vacuum UV

Atomic clocks – quantum logic readout



Most accurate and precise frequency standards – 8e-18 fractional uncertainty (Chou et al. PRL 104, 070802 (2010))

Trapped-ion summary



Have achieved quantum control of up to N ions

Have demonstrated all basic components required to create large scale entangled states

Algorithms & gates include Dense-coding, error-correction, Toffoli, Teleportation, Entanglement purification Entanglment swapping

Working on:

Higher precision

New manipulation methods

Scaling to many ions

